

Biases in Multi-GNSS Processing

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NGK Summer School

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Overview

Observation Equation

GNSS Code Biases

GNSS Phase Biases

Inter-System Antenna Bias

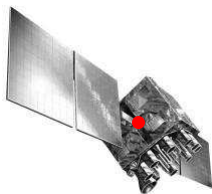
Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
$$L_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) \\ + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$



Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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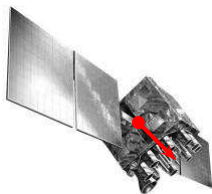


\vec{x}^k

position vector of satellite k related
to its center of mass

Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
$$L_i^k = |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_i + \Delta\vec{\chi}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) \\ + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$



\vec{x}^k

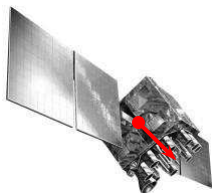
position vector of satellite k related to its center of mass

$\Delta\vec{x}^k, \Delta\vec{\chi}^k$

vector from the center of mass of the satellite k to the antenna signal emission point for code and phase observations

Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
$$L_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$



\vec{x}^k

position vector of satellite k related to its center of mass

$\Delta\vec{x}^k, \Delta\vec{\chi}^k$

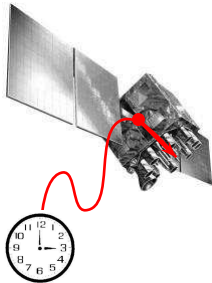
vector from the center of mass of the satellite k to the antenna signal emission point for code and phase observations

δ^k

clock correction of the satellite k with respect to GPS time

Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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\vec{x}^k

position vector of satellite k related to its center of mass

$\Delta\vec{x}^k, \Delta\vec{\chi}^k$

vector from the center of mass of the satellite k to the antenna signal emission point for code and phase observations

δ^k

clock correction of the satellite k with respect to GPS time

a^k, α^k

hardware delay in the satellite k for code and phase measurements

Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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I_i^k signal delay in the ionosphere



Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
$$L_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$



I_i^k signal delay in the ionosphere
 T_i^k signal delay in the troposphere

Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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δ_i

clock correction of the receiver at the station i with respect to GPS time



Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - a^k)$$
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δ_i

clock correction of the receiver at the station i with respect to GPS time

α_i, α_i

hardware delay in the receiver at the station i for code and phase measurements

Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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δ_i

clock correction of the receiver at the station i with respect to GPS time

a_i, α_i

hardware delay in the receiver at the station i for code and phase measurements

$\Delta\vec{x}_i, \Delta\vec{\chi}_i$

vector from the marker of the station i to the antenna signal reception point for code and phase observations



Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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δ_i

clock correction of the receiver at the station i with respect to GPS time

a_i, α_i

hardware delay in the receiver at the station i for code and phase measurements

$\Delta\vec{x}_i, \Delta\vec{\chi}_i$

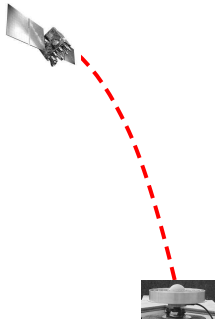
vector from the marker of the station i to the antenna signal reception point for code and phase observations

\vec{x}_i

position vector of marker at station i

Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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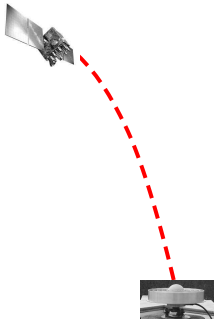


N_i^k

phase ambiguity (one and the same for one pass)

Observation Equation

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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N_i^k phase ambiguity (one and the same for one pass)

$\Delta\varphi_i^k$ initial phase shift between the oscillators at station i and satellite k

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$

Phase $\Delta\vec{\chi}_i$

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$ a_i

Phase $\Delta\vec{\chi}_i$ α_i

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
$$L_i^k = |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_i + \Delta\vec{\chi}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) \\ + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code	$\Delta\vec{x}_i$	a_i	δ^k
Phase	$\Delta\vec{\chi}_i$	α_i	δ^k

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code	$\Delta\vec{x}_i$	a_i	δ^k
Phase	$\Delta\vec{x}_i$	α_i	δ^k

ISB: Inter-System Bias

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
$$L_i^k = |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_i + \Delta\vec{\chi}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) \\ + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$ a_i δ^k

Phase $\Delta\vec{\chi}_i$ α_i δ^k

ISB: Inter-System Bias

Frequency: (f1 or f2 or fn for GLONASS or ...)

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$ a_i δ^k

Phase $\Delta\vec{\chi}_i$ α_i δ^k

ISB: Inter-System Bias

Frequency: (f1 or f2 or fn for GLONASS or ...)

Code $\Delta\vec{x}^k$

Phase $\Delta\vec{\chi}^k$

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$ a_i δ^k

Phase $\Delta\vec{\chi}_i$ α_i δ^k

ISB: Inter-System Bias

Frequency: (f1 or f2 or fn for GLONASS or ...)

Code $\Delta\vec{x}^k$ $\Delta\vec{x}_i$

Phase $\Delta\vec{\chi}^k$ $\Delta\vec{\chi}_i$

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$ a_i δ^k

Phase $\Delta\vec{\chi}_i$ α_i δ^k

ISB: Inter-System Bias

Frequency: (f1 or f2 or fn for GLONASS or ...)

Code $\Delta\vec{x}^k$ $\Delta\vec{x}_i$ a_i

Phase $\Delta\vec{\chi}^k$ $\Delta\vec{\chi}_i$ α_i

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$ a_i δ^k

Phase $\Delta\vec{\chi}_i$ α_i δ^k

ISB: Inter-System Bias

Frequency: (f1 or f2 or fn for GLONASS or ...)

Code $\Delta\vec{x}^k$ $\Delta\vec{x}_i$ a_i a^k

Phase $\Delta\vec{\chi}^k$ $\Delta\vec{\chi}_i$ α_i α^k

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

$$L_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$ a_i δ^k

Phase $\Delta\vec{\chi}_i$ α_i δ^k

ISB: Inter-System Bias

Frequency: (f1 or f2 or fn for GLONASS or ...)

Code $\Delta\vec{x}^k$ $\Delta\vec{x}_i$ a_i a^k

Phase $\Delta\vec{\chi}^k$ $\Delta\vec{\chi}_i$ α_i α^k

IFB: Inter-Frequency Bias

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

$$L_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code $\Delta\vec{x}_i$ a_i δ^k

Phase $\Delta\vec{\chi}_i$ α_i δ^k

ISB: Inter-System Bias

Frequency: (f1 or f2 or fn for GLONASS or ...)

Code $\Delta\vec{x}^k$ $\Delta\vec{x}_i$ a_i a^k

Phase $\Delta\vec{\chi}^k$ $\Delta\vec{\chi}_i$ α_i α^k

IFB: Inter-Frequency Bias

Signal type: (C1W/C or C2W/C or L2W/C or ...)

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

$$L_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code	$\Delta\vec{x}_i$	a_i	δ^k	ISB: Inter-System Bias
Phase	$\Delta\vec{\chi}_i$	α_i	δ^k	

Frequency: (f1 or f2 or fn for GLONASS or ...)

Code	$\Delta\vec{x}^k$	$\Delta\vec{x}_i$	a_i	a^k	IFB: Inter-Frequency Bias
Phase	$\Delta\vec{\chi}^k$	$\Delta\vec{\chi}_i$	α_i	α^k	

Signal type: (C1W/C or C2W/C or L2W/C or ...)

Code	a_i
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Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

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The following parameters depend on:

GNSS: (GPS or GLONASS or ...)

Code	$\Delta\vec{x}_i$	a_i	δ^k	ISB: Inter-System Bias
Phase	$\Delta\vec{\chi}_i$	α_i	δ^k	

Frequency: (f1 or f2 or fn for GLONASS or ...)

Code	$\Delta\vec{x}^k$	$\Delta\vec{x}_i$	a_i	a^k	IFB: Inter-Frequency Bias
Phase	$\Delta\vec{\chi}^k$	$\Delta\vec{\chi}_i$	α_i	α^k	

Signal type: (C1W/C or C2W/C or L2W/C or ...)

Code	a_i	a^k
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Frequency: (f1 or f2 or fn for GLONASS or ...)

Code	$\Delta\vec{x}^k$	$\Delta\vec{x}_i$	a_i	a^k	IFB: Inter-Frequency Bias
Phase	$\Delta\vec{\chi}^k$	$\Delta\vec{\chi}_i$	α_i	α^k	

Signal type: (C1W/C or C2W/C or L2W/C or ...)

Code	a_i	a^k	DCB: Differential Code Bias (Quarter cycle problem)
Phase	α_i	α^k	

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

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Code	a_i	a^k	DCB: Differential Code Bias
------	-------	-------	-----------------------------

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GNSS:

Code
Phase

$\Delta\vec{x}_i$
 $\Delta\vec{x}_i$

a_i
 α_i

δ^k
 δ^k

ISB: Inter-System Bias

Frequency:

Code
Phase

$\Delta\vec{x}^k$ $\Delta\vec{x}_i$
 $\Delta\vec{x}^k$ $\Delta\vec{x}_i$

a_i a^k
 α_i α^k

IFB: Inter-Frequency Bias

Signal type:

Code

a_i a^k

DCB: Differential Code Bias

GNSS Code Biases: Overview

If we focus on processing code measurements we have to consider:

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different hardware delays for P- and C-Code
bias at the receiver and satellite

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different hardware delays for measurements of different GNSS
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GNSS Code Biases: Overview

If we focus on processing code measurements we have to consider:

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different hardware delays for P- and C-Code
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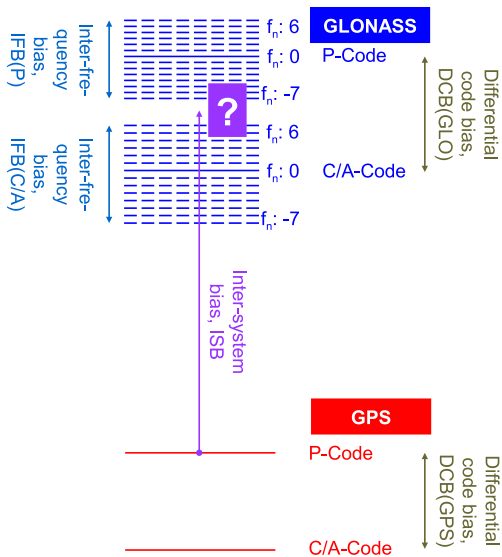
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different hardware delays for measurements of different GNSS
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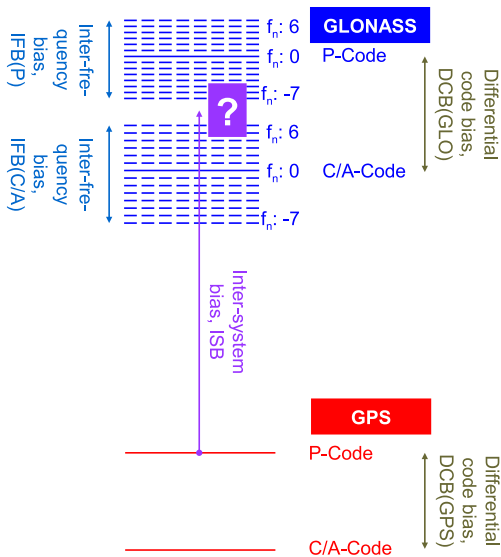
- **IFB: inter-frequency bias**

frequency-dependent hardware delays for the different
GLONASS-signals
bias at the receiver
(also at the satellite when frequency is changed)

GNSS Code Biases: Overview



GNSS Code Biases: Overview



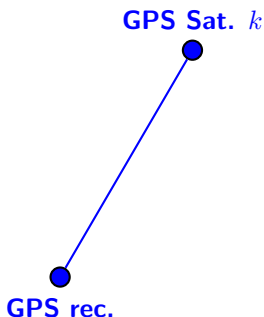
We can only extract the sum of delays from a GPS/GLONASS data processing.

Why do we Need These Biases?

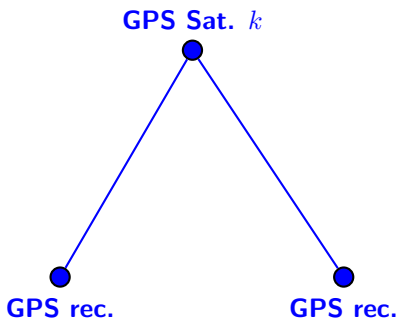
GPS Sat. k



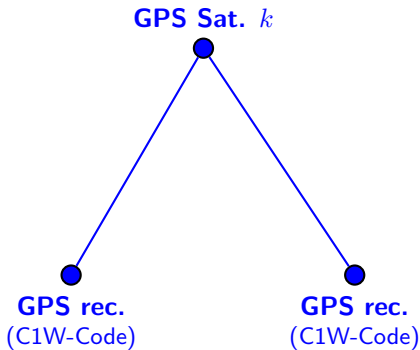
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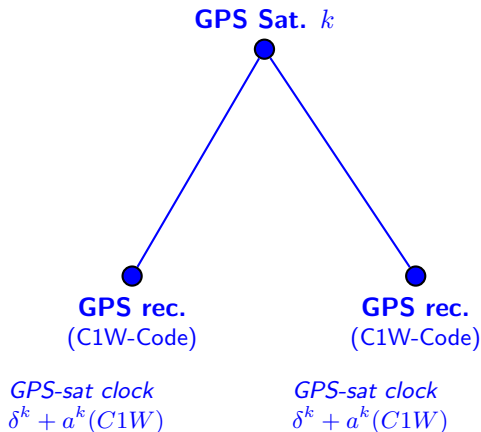
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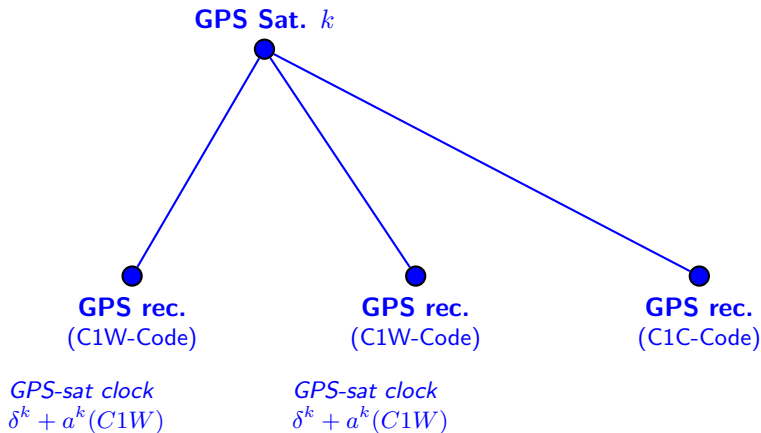
Why do we Need These Biases?



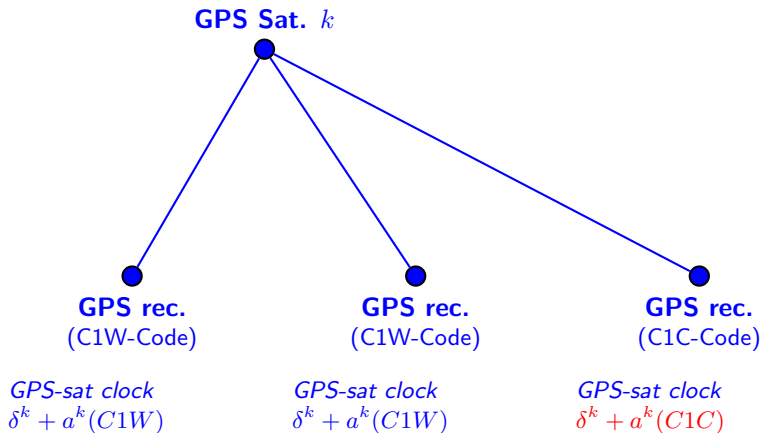
Why do we Need These Biases?



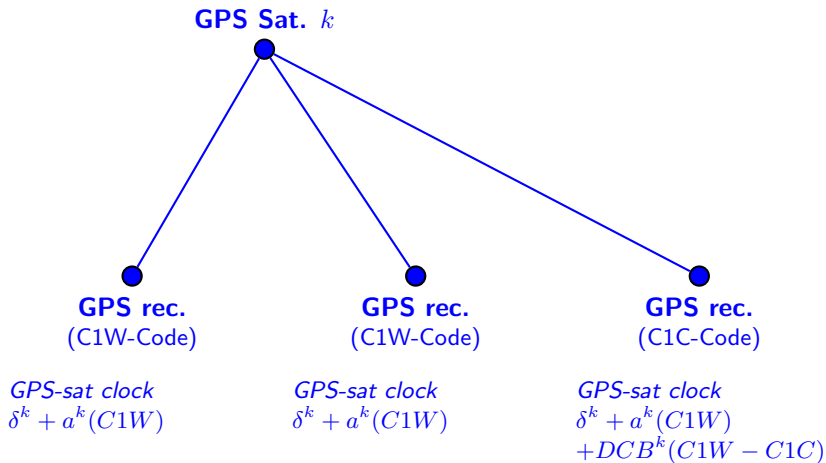
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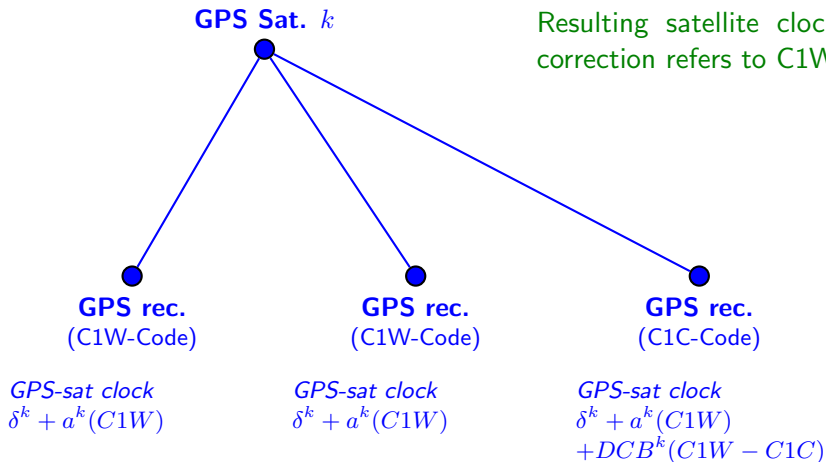


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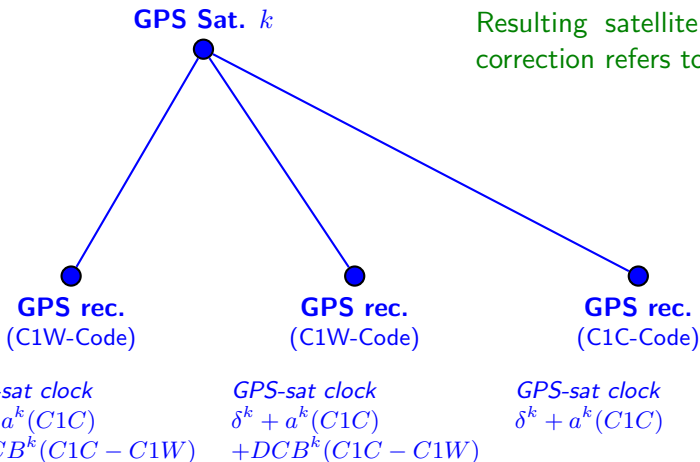
Why do we Need These Biases?

Resulting satellite clock correction refers to C1W



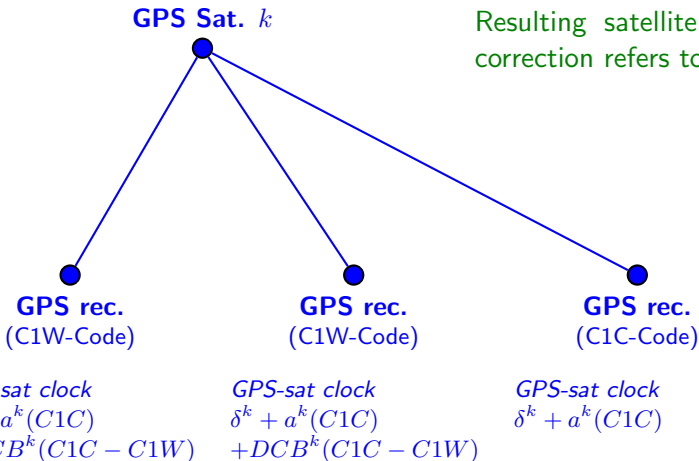
Why do we Need These Biases?

Resulting satellite clock correction refers to C1C



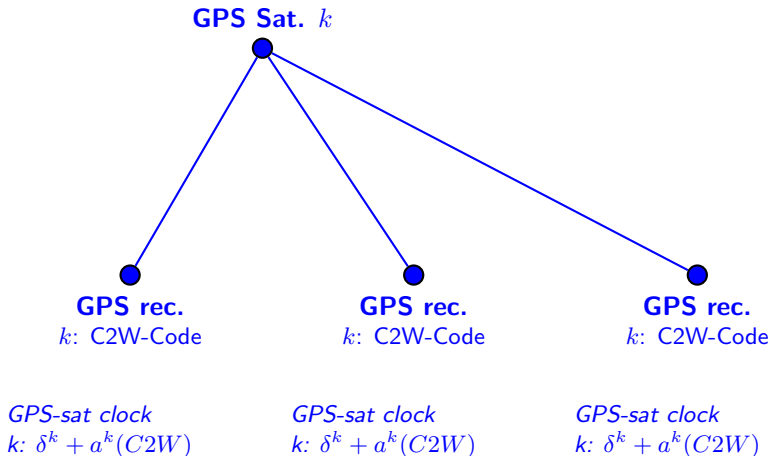
Why do we Need These Biases?

Resulting satellite clock correction refers to C1C

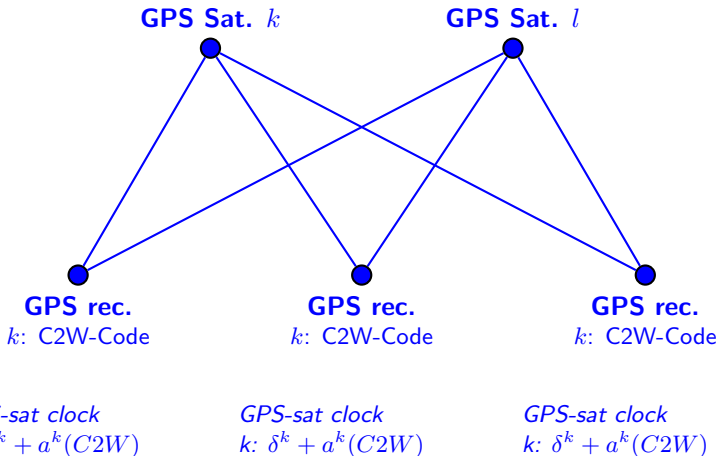


Whether choosing C1W or C1C as reference is fully equivalent.
Choosing C1C or C1W for the satellite clock is purely conventional.
The IGS products refer to the P-Code for the satellite clocks.

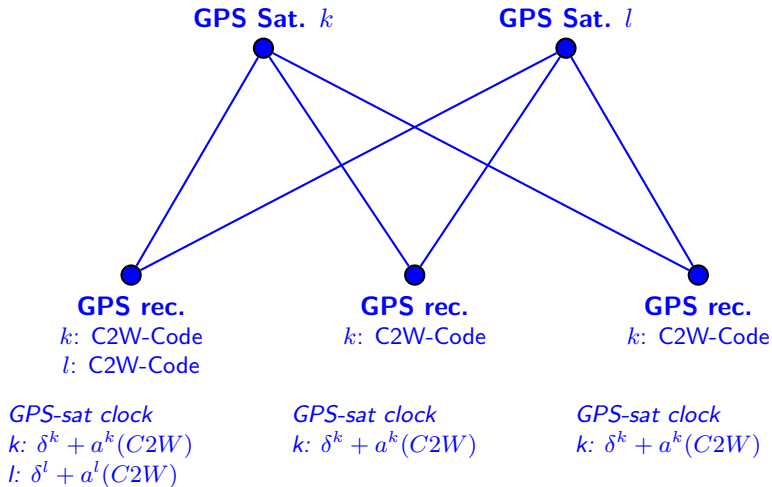
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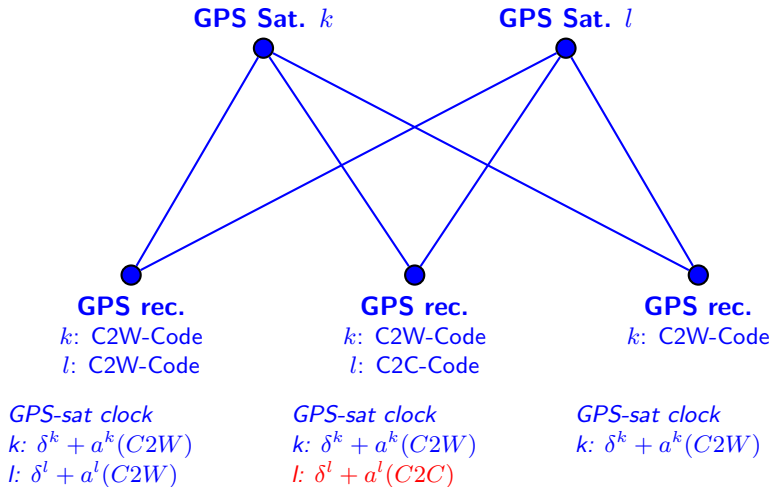
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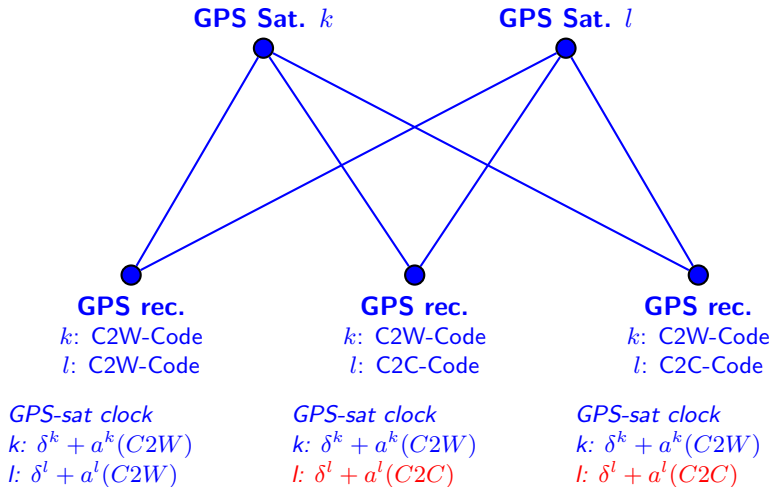
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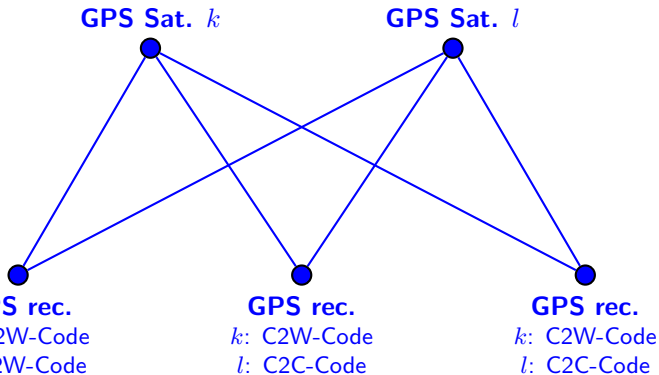
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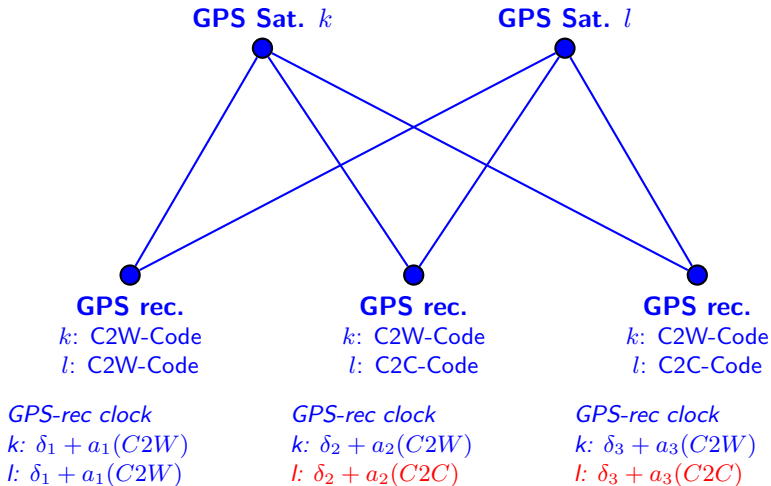


GPS-sat clock
 k : $\delta^k + a^k(C2W)$
 l : $\delta^l + a^l(C2W)$

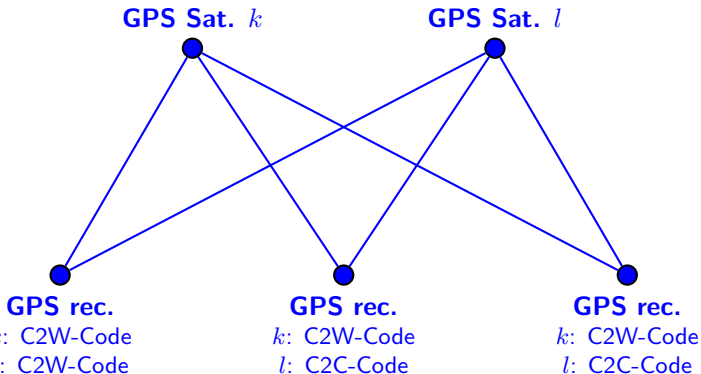
GPS-sat clock
 k : $\delta^k + a^k(C2W)$
 l : $\delta^l + a^l(C2W) +$
 $DCB^l(C2W - C2C)$

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Why do we Need These Biases?



GPS-rec clock
 $k: \delta_1 + a_1(C2W)$
 $l: \delta_1 + a_1(C2W)$

GPS-rec clock
 $k: \delta_2 + a_2(C2W)$
 $l: \delta_2 + a_2(C2W) +$
 $DCB_2(C2W - C2C)$

GPS-rec clock
 $k: \delta_3 + a_3(C2W)$
 $l: \delta_3 + a_3(C2W) +$
 $DCB_3(C2W - C2C)$

Code Biases in a GPS Network Solution

Depending on the code measurements of the individual receivers we can get:

- C1W-C1C or P1–C1 DCBs for all GPS satellites,
- C2W-C2C or P2–C2 DCBs for Block IIR-M (or later) satellites,
- C2W-C2C or P2–C2 DCBs for receivers if it tracks GPS satellites with P- and C-code on the second frequency at the same time.

Code Biases in a GPS Network Solution

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As soon as we get a mixture between all these observation types in one network solution we need

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- either to correct the DCBs in the data processing

Code Biases in a GPS Network Solution

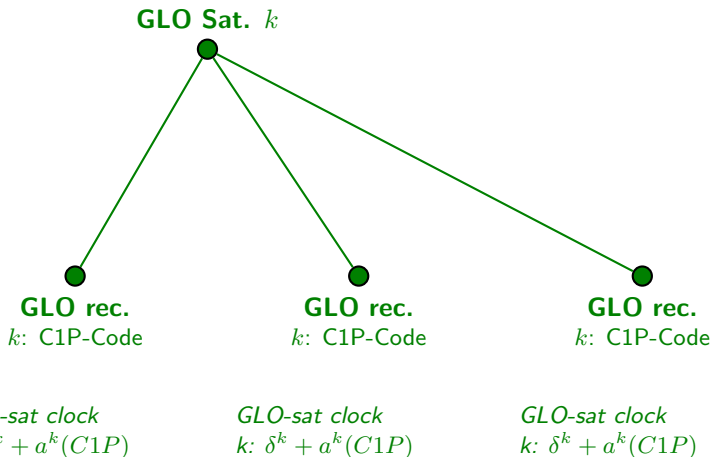
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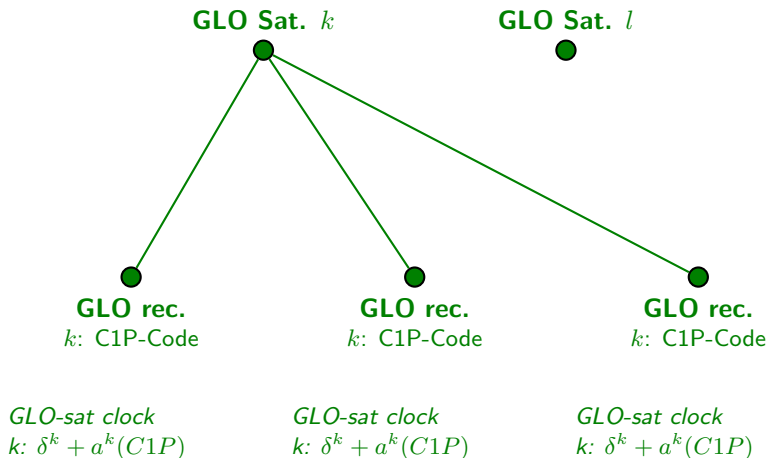
As soon as we get a mixture between all these observation types in one network solution we need

- either to correct the DCBs in the data processing
 - or to estimate DCB parameters
- P1–C1:** Your reference clock only belongs to either the P- or C/A-code class – **you need an additional reference for the satellite related biases.**
- P2–C2:** You have these DCBs at the satellites and receivers at the same time – **you need additional references for the satellite and receiver related biases.**

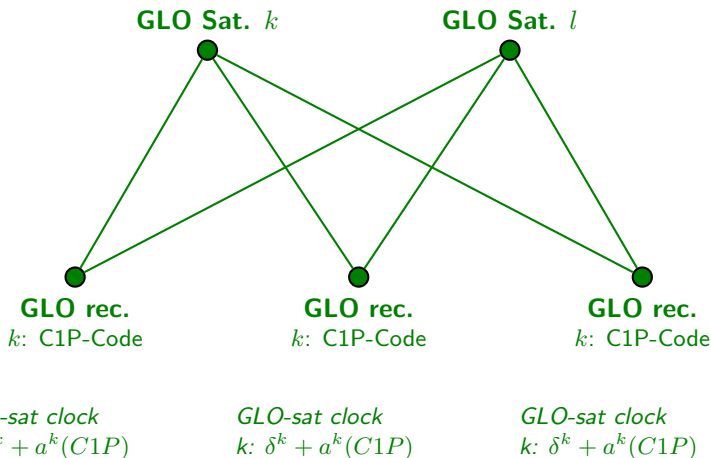
Why do we Need These Biases?



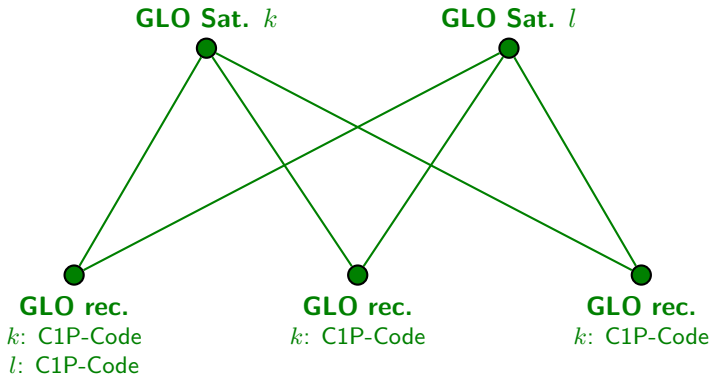
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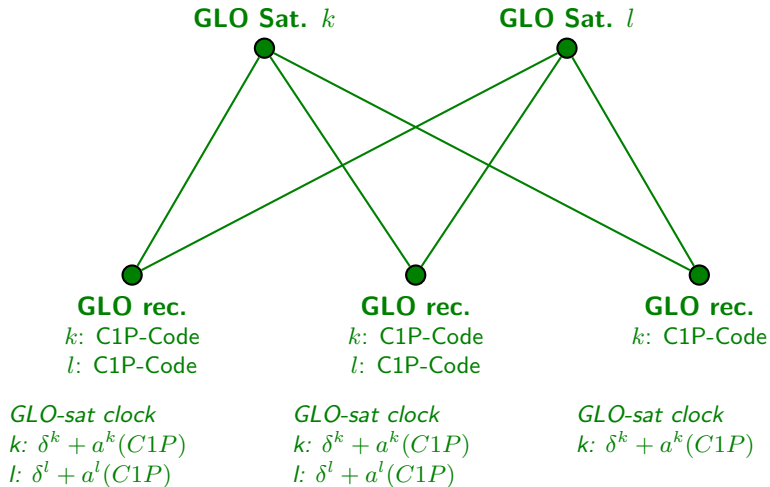


GLO-sat clock
 $k: \delta^k + a^k(C1P)$
 $l: \delta^l + a^l(C1P)$

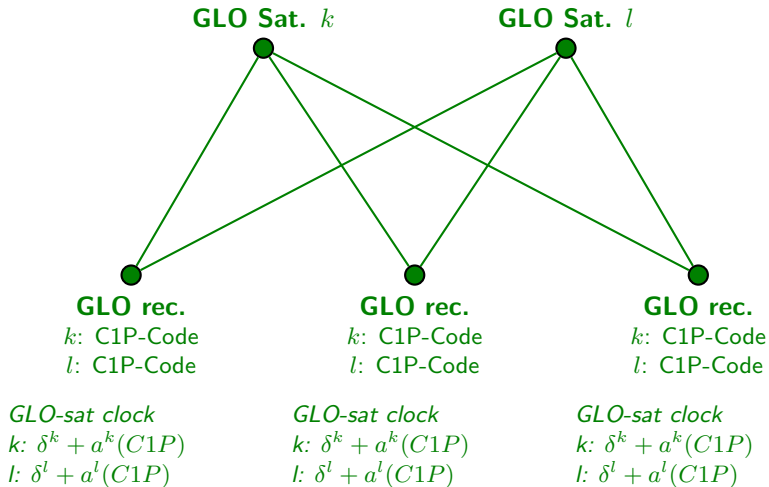
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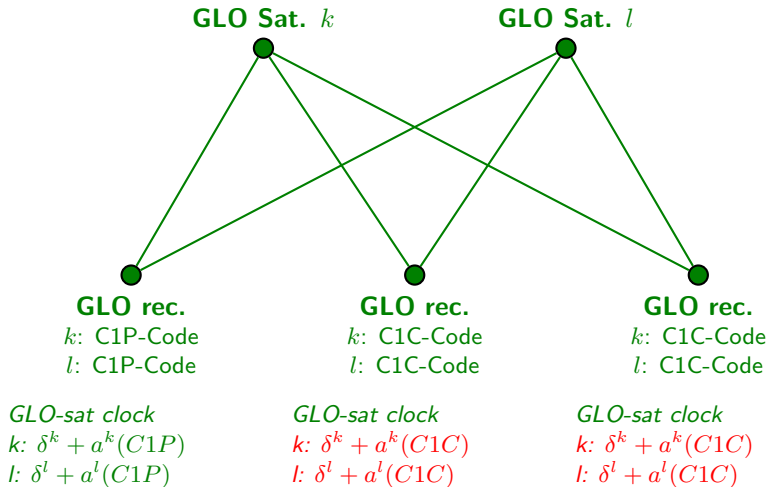
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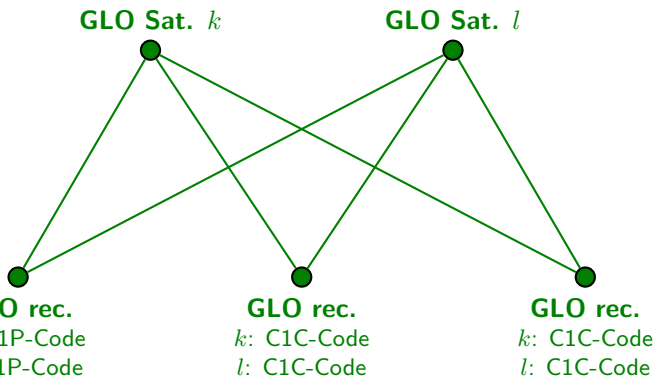
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GLO-sat clock

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GLO-sat clock

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$$DCB^k(C1P - C1C)$$

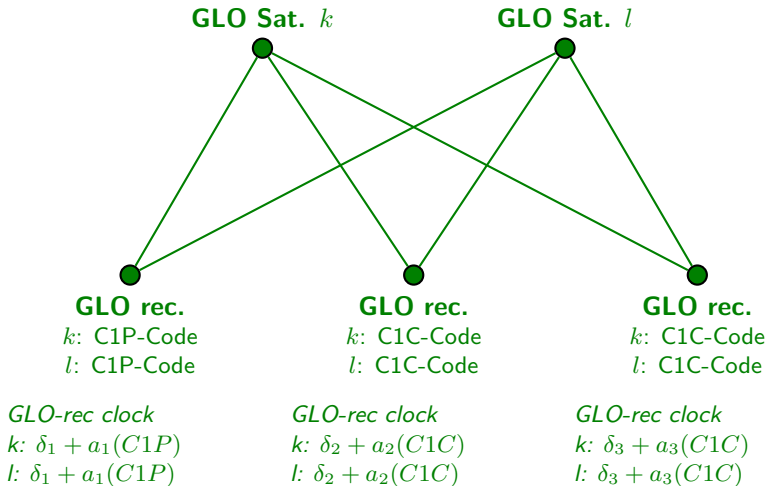
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GLO-sat clock

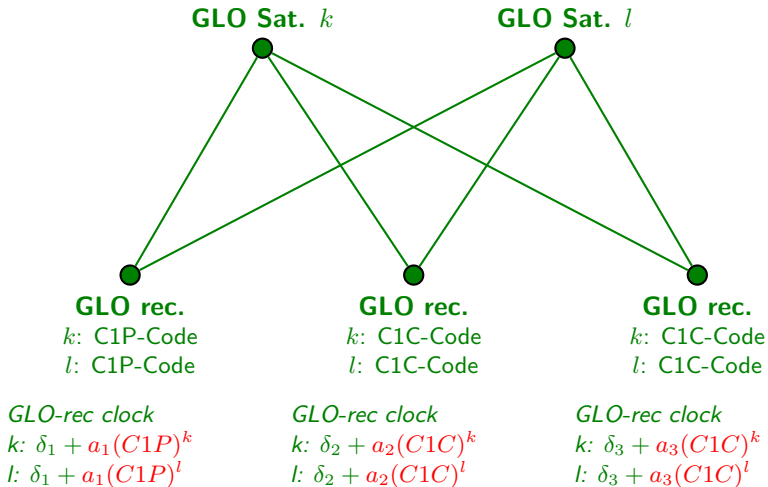
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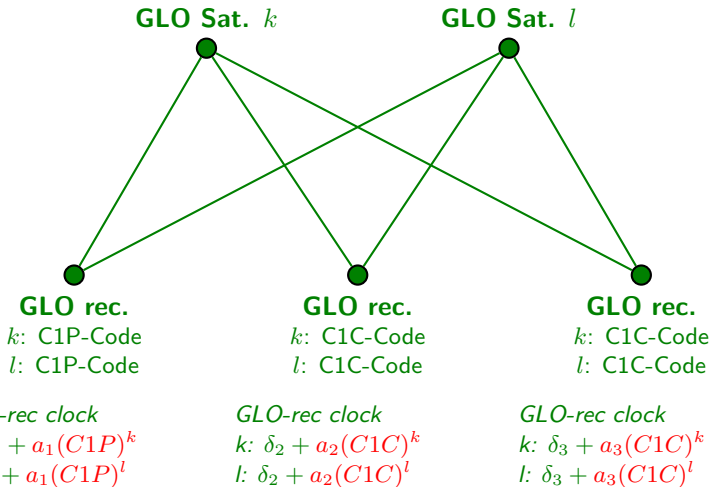
Why do we Need These Biases?



Why do we Need These Biases?



Why do we Need These Biases?



Because each GLONASS satellite emits the signal on its own frequency the receiver hardware delays become (satellite-)frequency-dependent.

Code Biases in a GLONASS Network Solution

Depending on the code measurements of the individual receivers we can get:

- $C1P - C1C$ or $P1 - C1$ DCBs for all GLONASS satellites,
- $C2P - C2C$ or $P2 - C2$ DCBs for all GLONASS satellites.

Code Biases in a GLONASS Network Solution

Depending on the code measurements of the individual receivers we can get:

- C1P–C1C or P1–C1 DCBs for all GLONASS satellites,
- C2P–C2C or P2–C2 DCBs for all GLONASS satellites.

As soon as we get a mixture between all these observation types in one network solution we need

- either to correct the DCBs in the data processing
 - or to estimate DCB parameters
- P1–C1 and P2–C2: Your reference clock only belongs to either the P- or C-code class – you need an additional reference for the satellite related biases.

Code Biases in a GLONASS Network Solution

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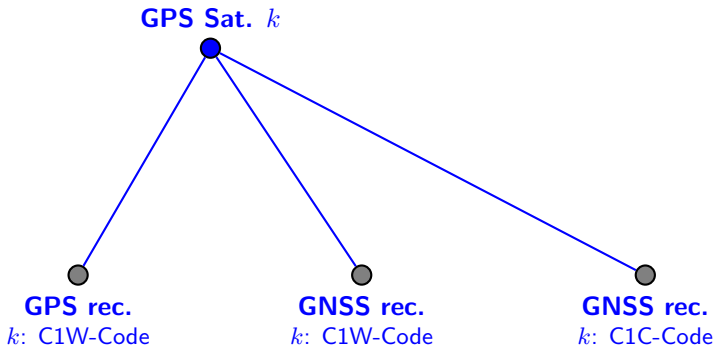
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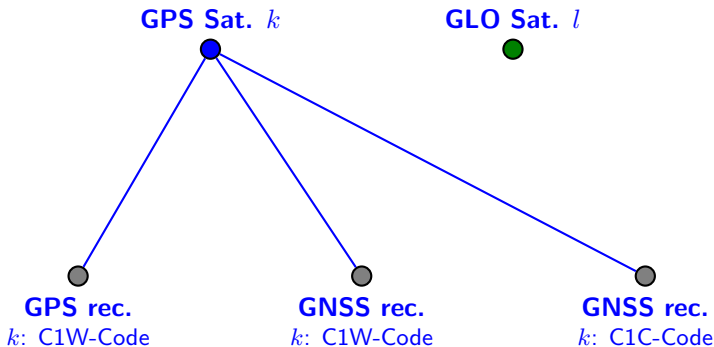
- either to correct the DCBs in the data processing
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- P1–C1 and P2–C2:** Your reference clock only belongs to either the P- or C-code class – you need an additional reference for the satellite related biases.

We also need to consider in addition an **inter-frequency bias (IFB)** because each GLONASS satellite emits the signal on another frequency.

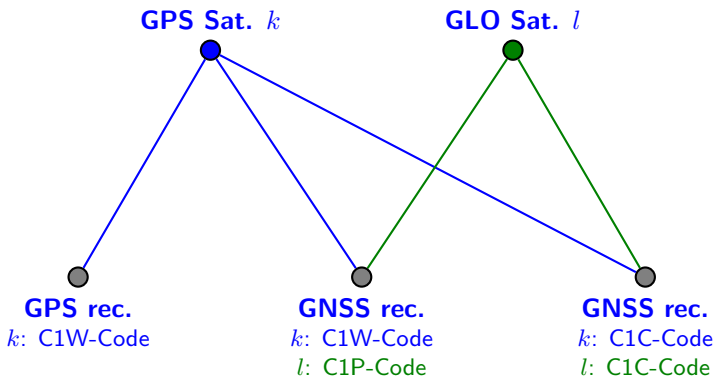
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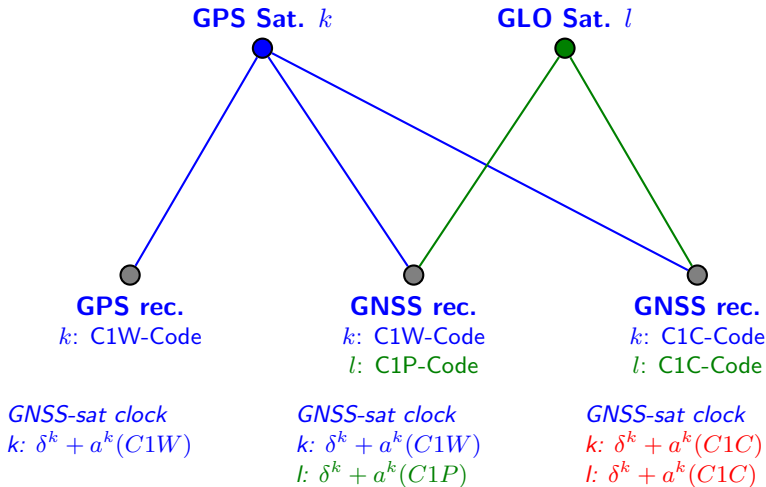
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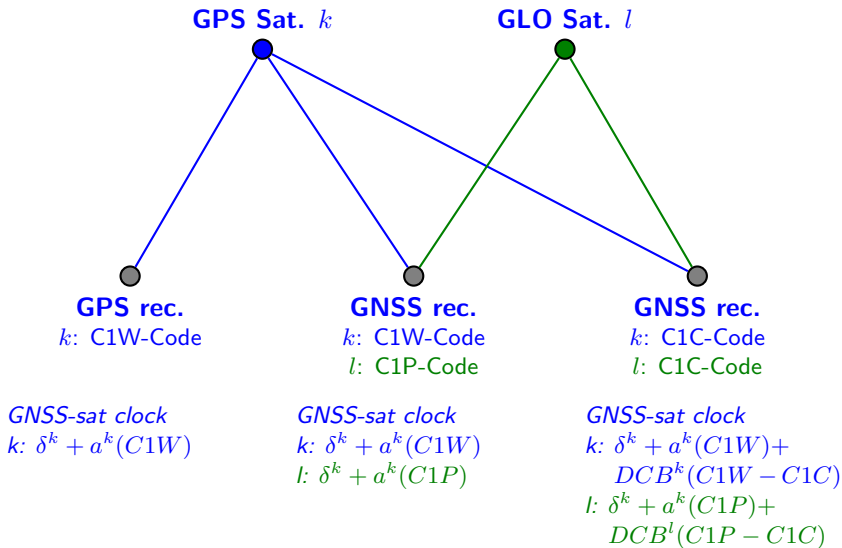
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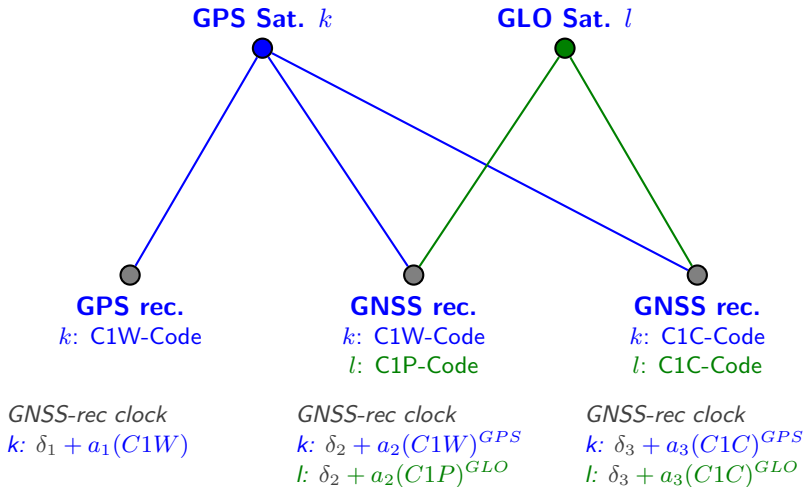
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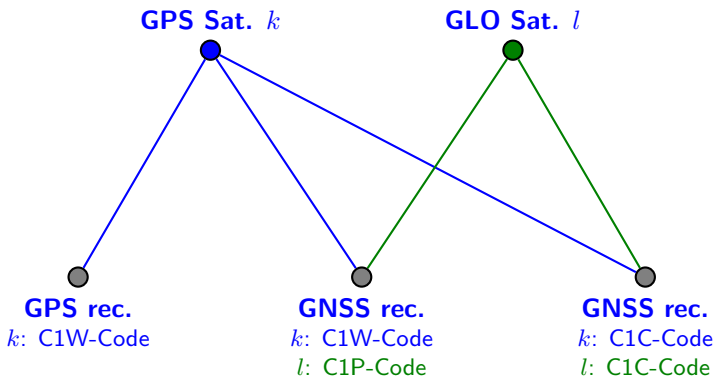
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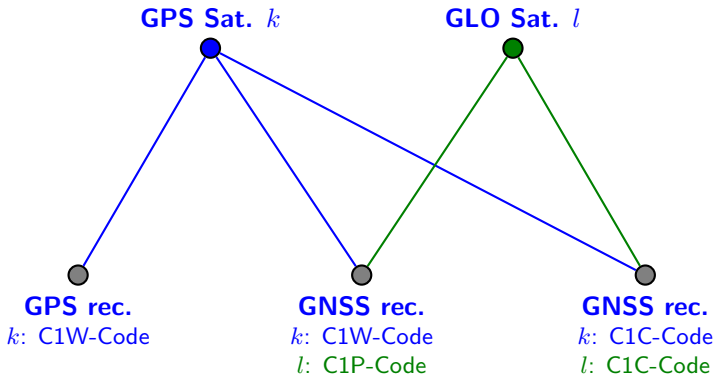


GNSS-rec clock
 $k: \delta_1 + a_1(C1W)$

GNSS-rec clock
 $k: \delta_2 + a_2(C1W)^{GPS}$
 $l: \delta_2 + a_2(C1P)^{GPS} +$
 $ISB_2(C1P)^{GPS-GLO}$

GNSS-rec clock
 $k: \delta_3 + a_3(C1C)^{GPS}$
 $l: \delta_3 + a_3(C1C)^{GPS} +$
 $ISB_3(C1C)^{GPS-GLO}$

Why do we Need These Biases?



GNSS-rec clock
 k : $\delta_1 + a_1(C1W)$

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 $ISB_3(C1C)^{GPS-GLO}$

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References are needed for

- P1-C1 DCB for GPS satellites,
- P2-C2 DCB for GPS satellites and GPS receivers tracking C2C,
- ISB for combined GPS/GLONASS tracking receivers,
- IFB for GLONASS tracking receivers.

Biases in a GPS/GLONASS Network Solution

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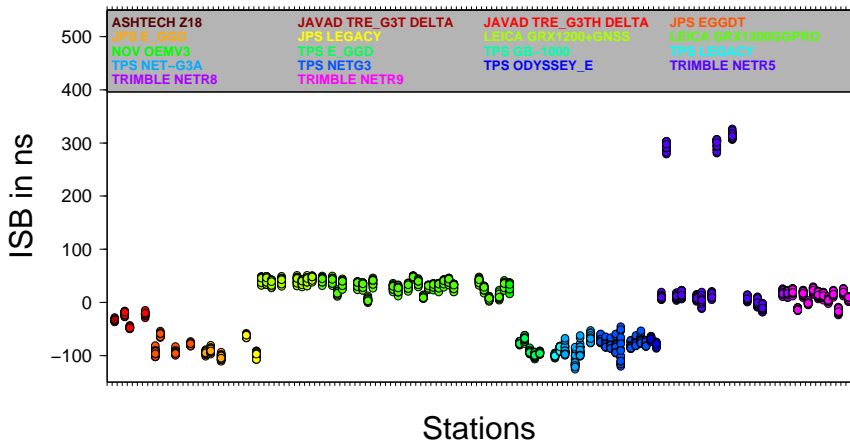
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Typical examples are:

- Receiver/satellite clock estimation in a zero-difference network solution.
- Melbourne-Wübbena linear combination for ambiguity resolution (even in the double-difference analysis).

IFB/ISB Comparisons

ISB characteristic of the receivers

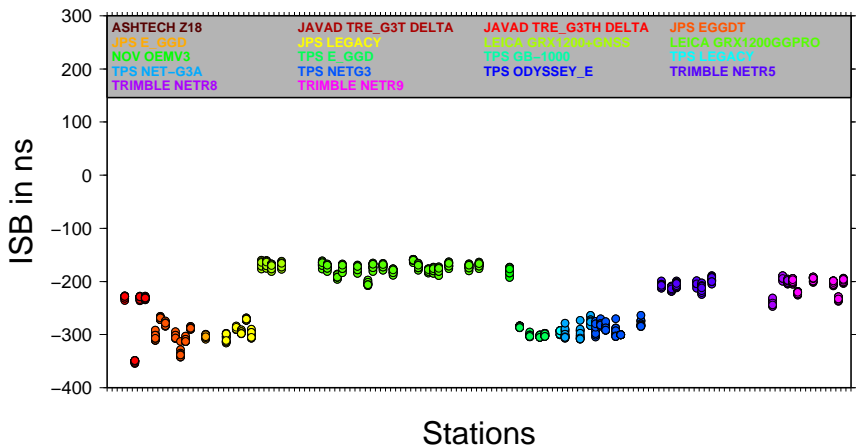


IFB/ISB computed by CODE

Test solution submitted to the IGS workshop on GNSS biases in January 2012

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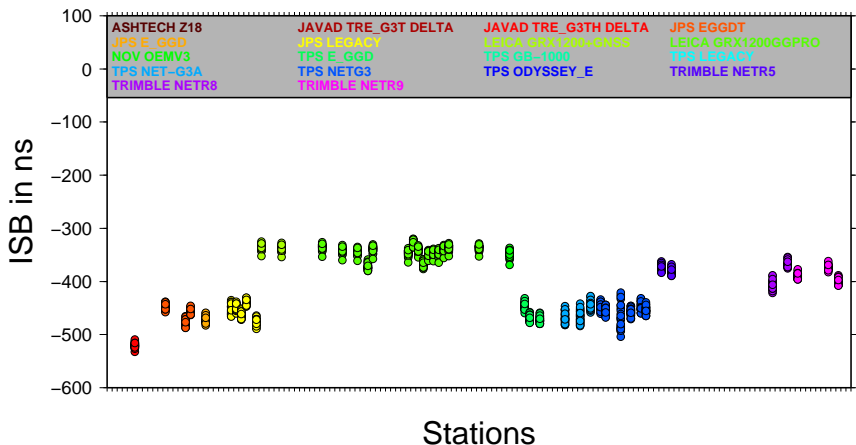


IFB/ISB computed by GFZ

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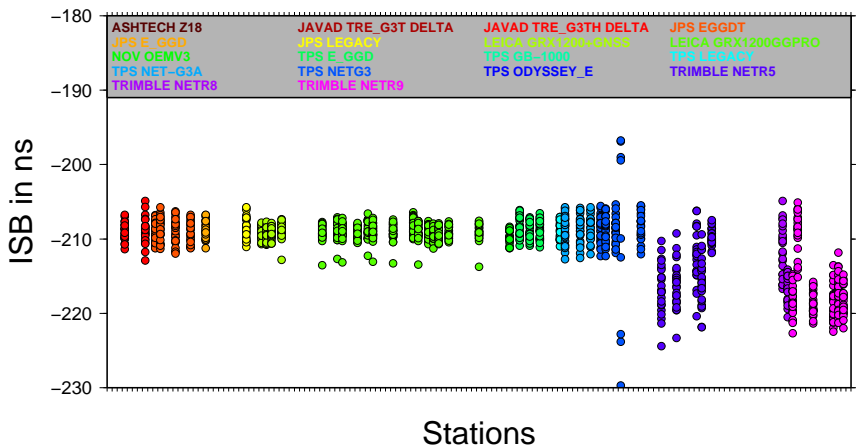


IFB/ISB computed by ESA

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IFB/ISB Comparisons

Differences between ISB characteristic of the receivers

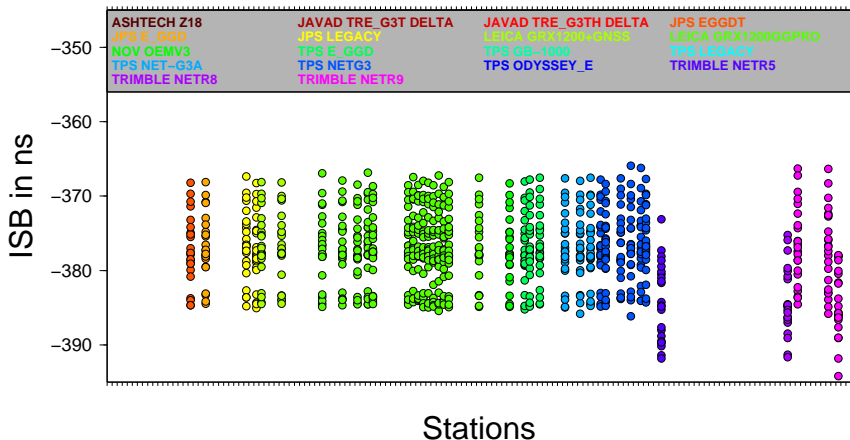


IFB/ISB computed by COD-GFZ

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IFB/ISB Comparisons

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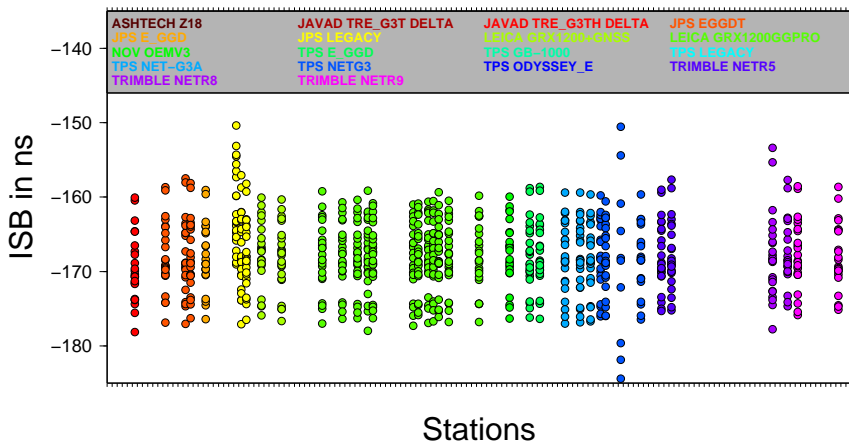


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IFB/ISB Comparisons

Differences between ISB characteristic of the receivers

Difference	Num. of Stations	Mean in ns	Median in ns	RMS in ns
CODE – GFZ	52	–210.6	–209.4	4.9
CODE – ESA	39	–377.5	–377.6	5.1
GFZ – ESA	36	–167.7	–168.2	6.1
CODE – GRGS	50	–371.9	–372.2	18.7
GFZ – GRGS	46	–162.1	–163.0	19.2
ESA – GRGS	34	6.1	5.8	20.6

- High consistency (low RMS) with a proper IFB–handling (enough weight for the code measurements?)
- Test whether the ACs select the same type of code observations (CODE differs from ESA and GFZ)

Further Code Biases

- When forming **linear combinations** from the P1 and P2 measurements

$$LC = \kappa_1 \cdot P_1 + \kappa_2 \cdot P_2$$

the original P1–C1, P2–C2 DCB values have to be applied with the corresponding coefficients:

$$DCB(LC) = \kappa_1 \cdot DCB(P1 - C1) + \kappa_2 \cdot DCB(P2 - C2)$$

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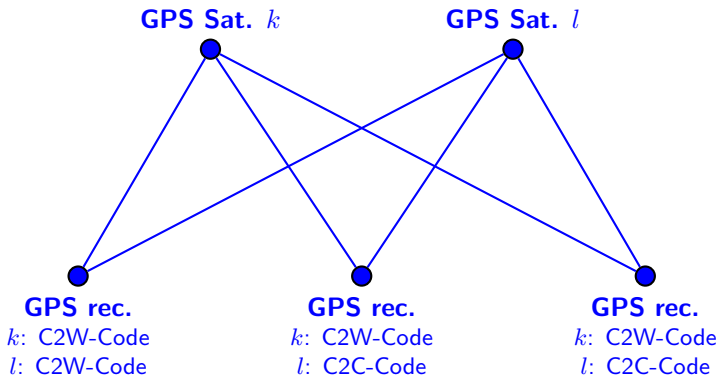
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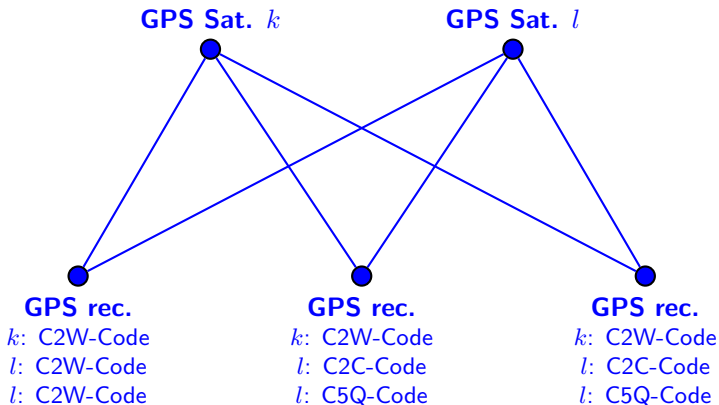
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- When extracting the **ionosphere information** by a linear combination, the differences between the hardware delays for P1 and P2 at the receiver and satellite need to be considered as an additional type of DCBs: **DCB(P1-P2)**
- With more GNSS and their new signals **more groups of Code Biases** will become relevant (e.g, third frequency for GPS and GLONASS).

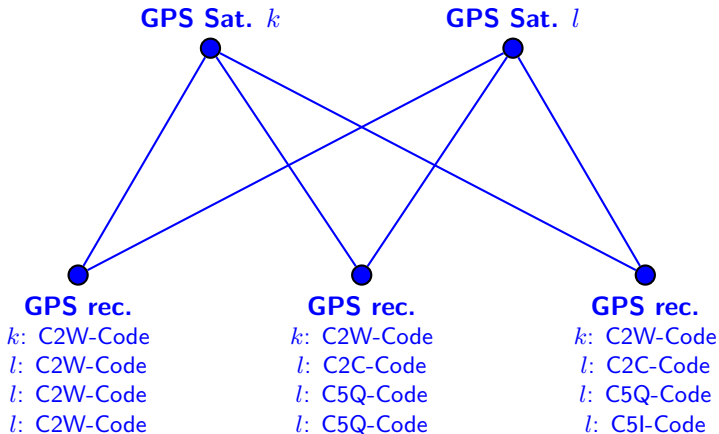
Why do we Need These Biases?



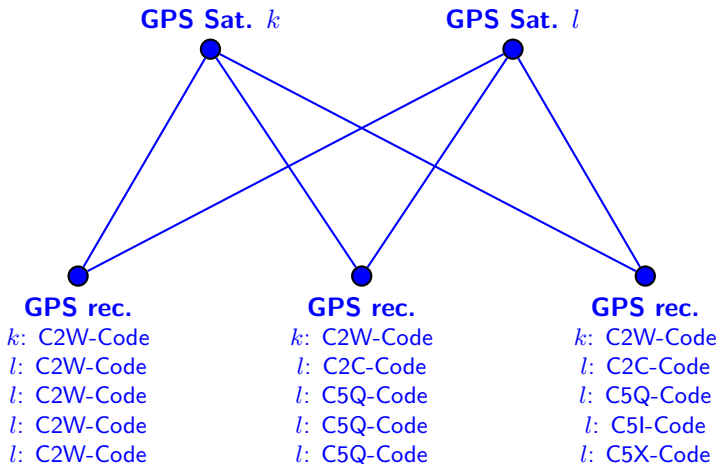
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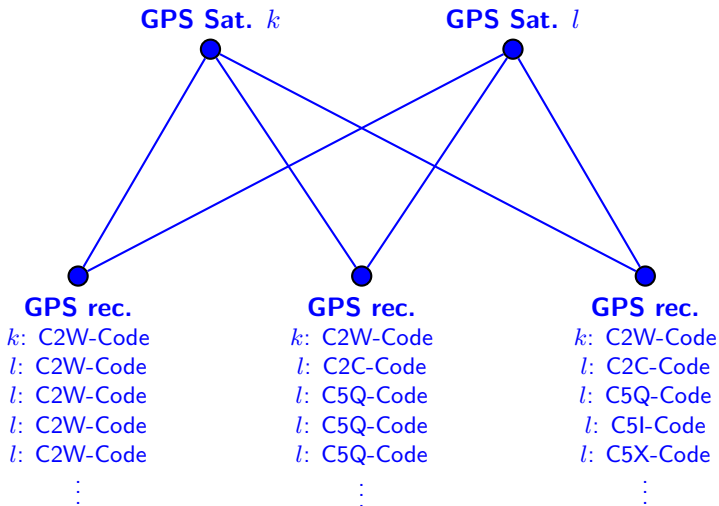
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Bias Handling in a Multi-GNSS Environment

If you simply follow the recipe from the classical examples you will end up with a long list of DCBs:

$$DCB^l(C2C - C2W), DCB^l(C5Q - C2W), \\ DCB^l(C5I - C2W), DCB^l(C5X - C2W), \dots$$

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- C5X is a mixture of C5Q- and C5I-signal that is not further specified by the manufacturers.
It must be expected that it is different for receivers from different manufacturers (firmware?).

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The **different DCBs are dependent** from each other:
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- Please be reminded that also receiver DCBs may be relevant.
- **It is urgently time to look for an alternative concept!**

Bias Handling in a Multi-GNSS Environment

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
$$L_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) \\ + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

Each code measurement P_i^k refers to two hardware delay terms: a_i for the receiver and a^k for the satellite.

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When processing linear combinations of the original observations each observation contributes to **four OSB parameters**.

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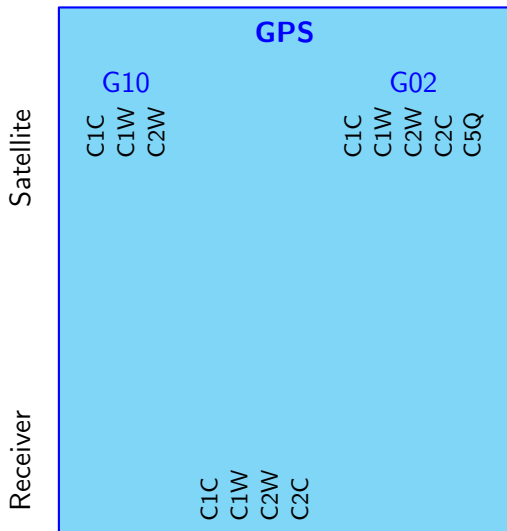
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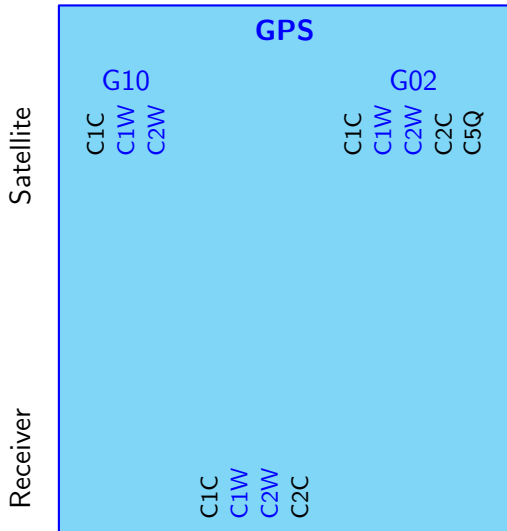
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Contributions from these sources can even be combined into one system of OSB parameters.

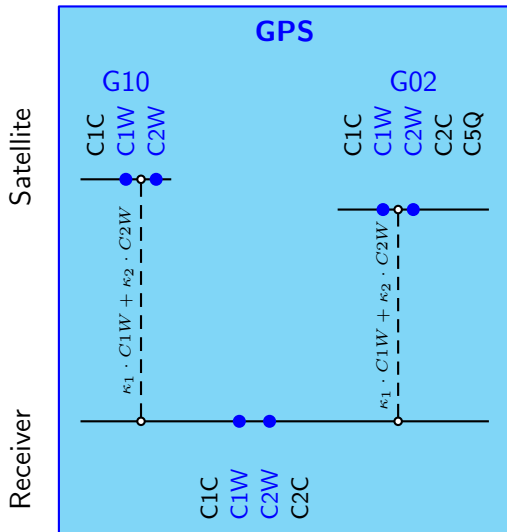
Pseudo-Absolute Code Biases: CLK



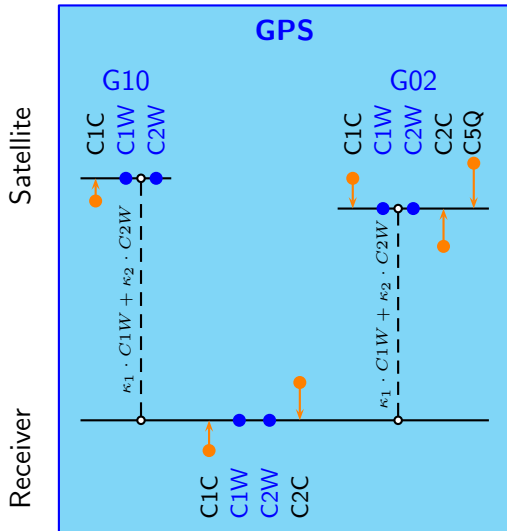
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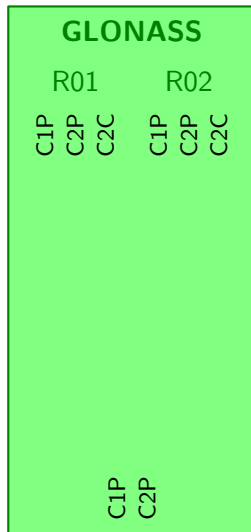
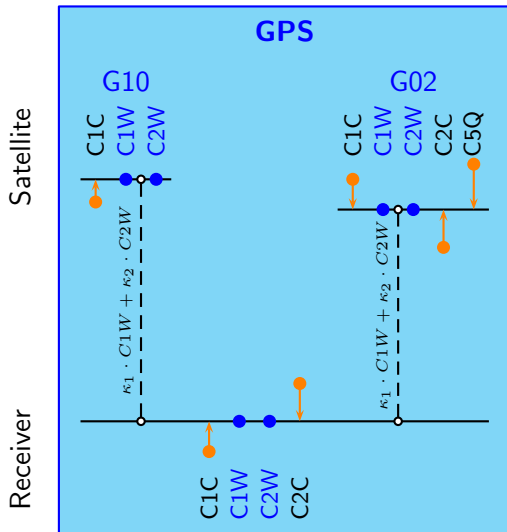
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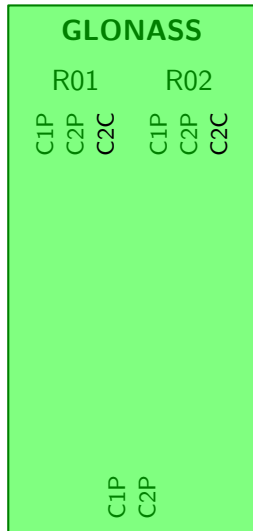
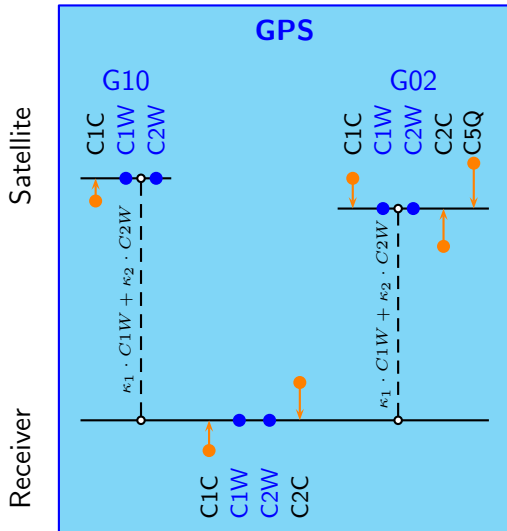
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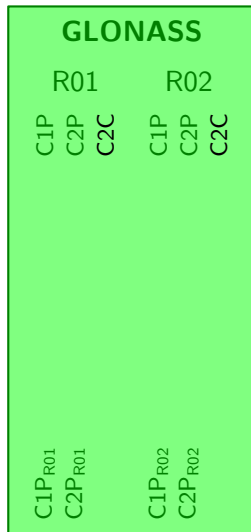
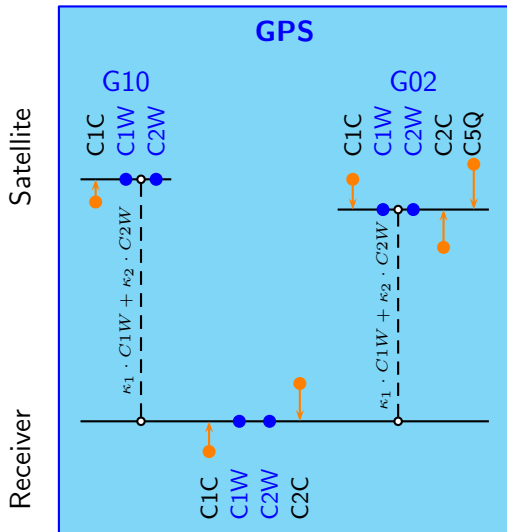
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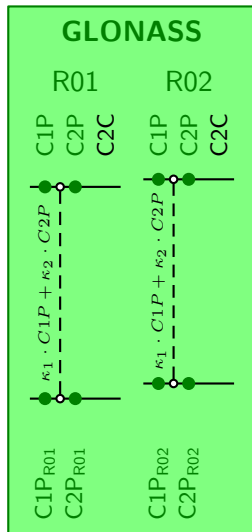
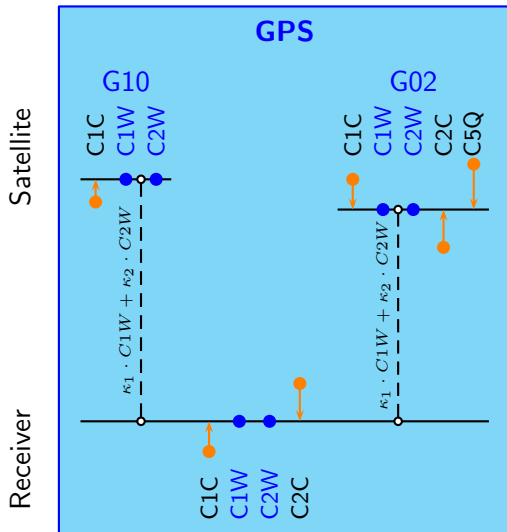
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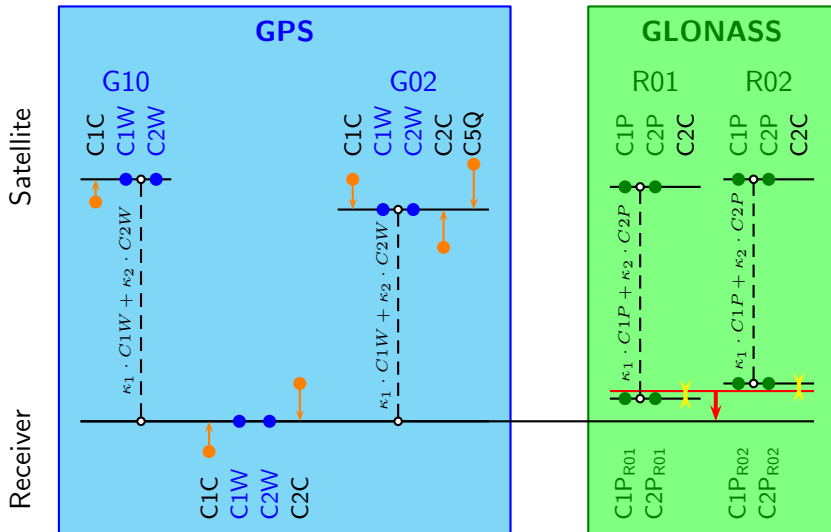
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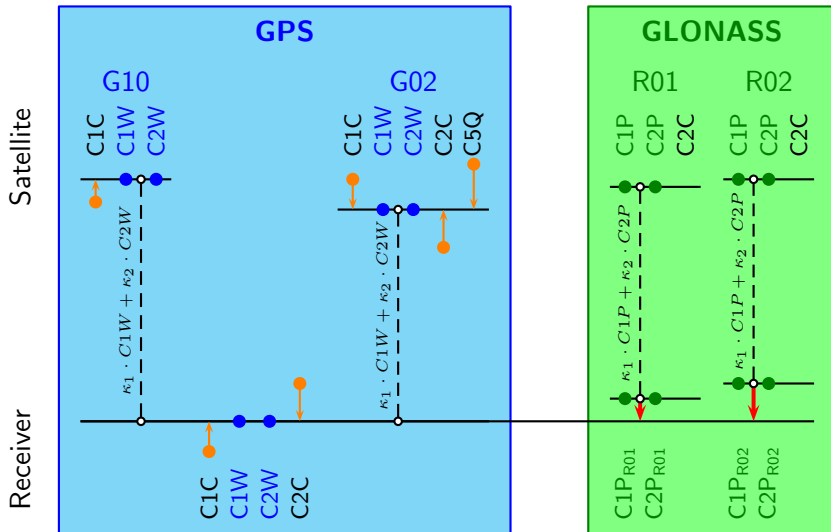
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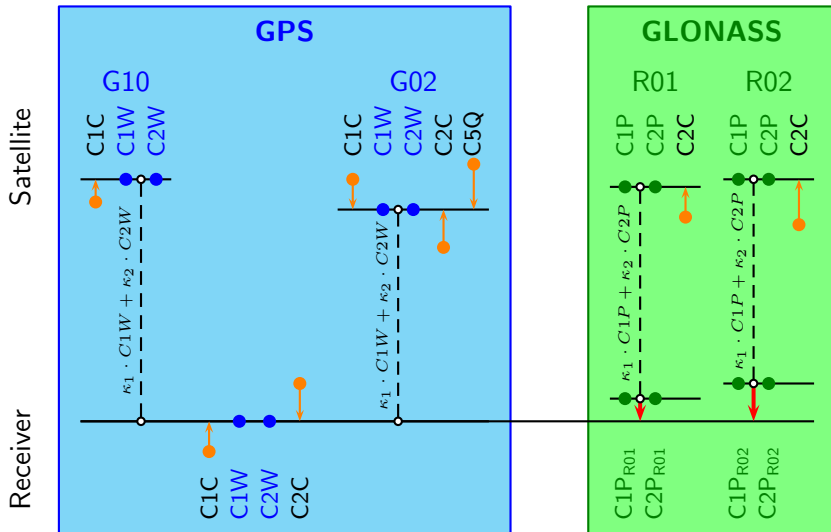
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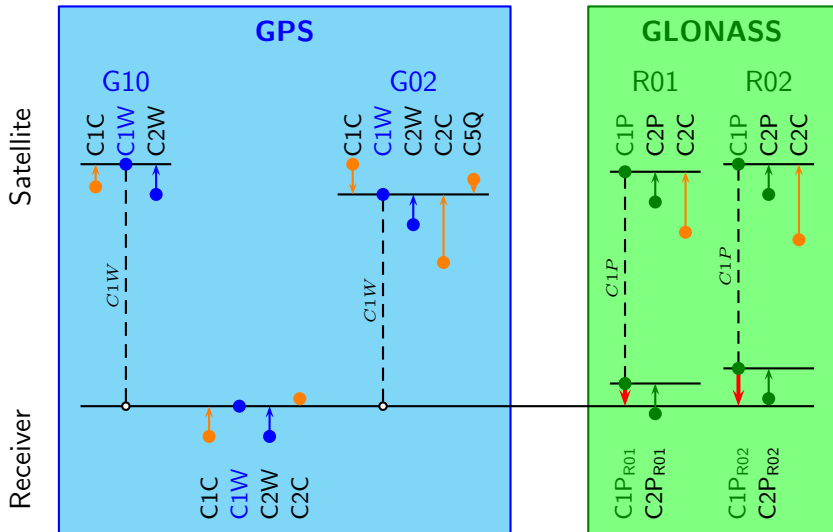
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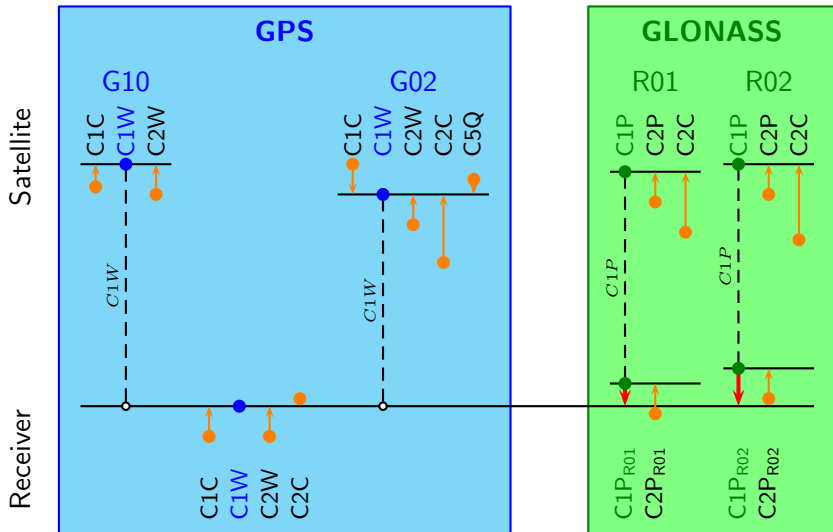
Pseudo-Absolute Code Biases: CLK



Pseudo-Absolute Code Biases: CLK+ION

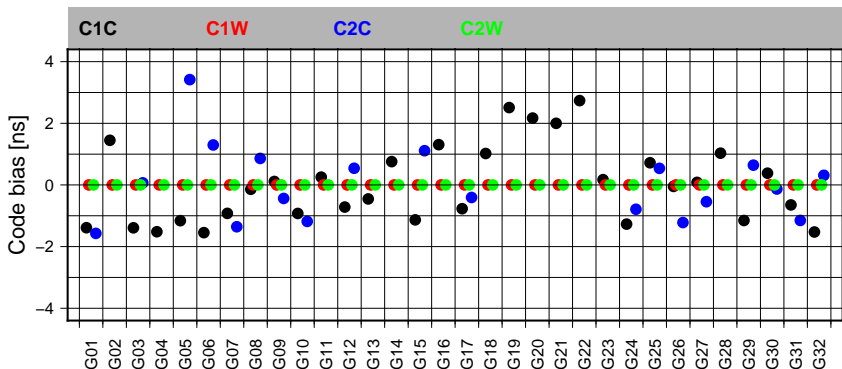


Pseudo-Absolute Code Biases: CLK+ION



Pseudo-Absolute Code Biases

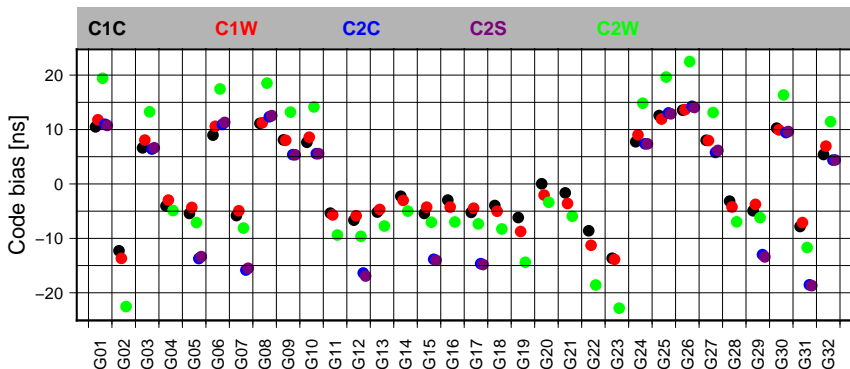
Estimated bias parameters from the CODE MGEX solution



Bias solution for GPS satellites based only on CLK:
reference ionosphere-free linear combination from C1W/C2W
(only biases for the satellites have been estimated)

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Estimated bias parameters from the CODE MGEX solution



Bias solution for GPS satellites based only on CLK+ION: [reference C1W](#)

(also biases for all stations are estimated)

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Estimation of Code Biases

The Reference signal for IGS products is defined by:

$$a(LC_{ion-free}) = \kappa_1 \cdot a(P1 - Code) + \kappa_2 \cdot a(P2 - Code)$$

If a receiver provides alternative measurements, DCB corrections need to be applied.

Examples:

- Receiver is tracking C1C/C2D=L1(C/A)+(P2-P1):
 - Correction for the second frequency:

$$\underbrace{DCB(P1 - C1) - DCB(P1 - P2)}_{L1(C/A)} + \underbrace{0}_{P2} - \underbrace{DCB(P2 - P1)}_{P1}$$

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$$DCB(P1 - C1) - DCB(P1 - P2) + 0 + DCB(P1 - P2)$$

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Examples:

- Receiver is tracking $C1C/C2D = L1(C/A) + (P2 - P1)$:
 - Correction for the second frequency:

$$DCB(P1 - C1)$$

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Examples:

- Receiver is tracking **C1C**/C2D=L1(C/A)+(P2-P1):
 - Correction for the second frequency: DCB(P1-C1)
 - Correction for the first frequency: DCB(P1-C1)

Estimation of Code Biases

The Reference signal for IGS products is defined by:

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If a receiver provides alternative measurements, DCB corrections need to be applied.

Examples:

- Receiver is tracking $C1C/C2D = L1(C/A) + (P2 - P1)$:
 - Correction for the second frequency: $DCB(P1 - C1)$
 - Correction for the first frequency: $DCB(P1 - C1)$
 - Combining the corrections from the two frequencies:

$$\kappa_1 \cdot DCB(P1 - C1) + \kappa_2 \cdot DCB(P1 - C1)$$

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 - Correction for the second frequency: $DCB(P1 - C1)$
 - Correction for the first frequency: $DCB(P1 - C1)$
 - Combining the corrections from the two frequencies:

$$\kappa_1 \cdot DCB(P1 - C1) + \kappa_2 \cdot DCB(P1 - C1) = \textcolor{red}{DCB(P1 - C1)}$$

Estimation of Code Biases

When estimating DCBs the receiver classes must be distinguished as derived before:

- Receiver is tracking C1W/C2W:
 $0 \cdot DCB(P1 - C1)$
- Receiver is tracking C1C/C2W:
 $\kappa_1 \cdot DCB(P1 - C1)$
- Receiver is tracking C1C/C2D=L1(C/A)+(P2-P1):
 $1 \cdot DCB(P1 - C1)$

Estimation of Code Biases

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- Receiver is tracking C1W/C2W:

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- Receiver is tracking C1C/C2W:

$$\kappa_1 \cdot DCB(P1 - C1)$$

- Receiver is tracking C1C/C2D=L1(C/A)+(P2-P1):

$$1 \cdot DCB(P1 - C1)$$

In order to estimate the $DCB(P1 - C1)$, the **factors** are used as partial derivatives in the least squares adjustment process.

Estimation of Code Biases

When estimating DCBs the receiver classes must be distinguished as derived before:

- Receiver is tracking C1W/C2W:

$$0 \cdot DCB(P1 - C1)$$

- Receiver is tracking C1C/C2W:

$$\kappa_1 \cdot DCB(P1 - C1)$$

- Receiver is tracking C1C/C2D=L1(C/A)+(P2-P1):

$$1 \cdot DCB(P1 - C1)$$

If the $DCB(P1 - C1)$ is known the **pre-factor** can be estimated and the tracking technology of the receiver can be detected/verified.

Estimation of Code Biases

Station		Estimated factor	Sigma	Related tracking	Receiver	Receiver tracking	
GANP	11515M001	2.826	0.021	C1/P2	TRIMBLE NETR8	C1/P2	OK
HERT	13212M010	2.503	0.019	C1/P2	LEICA GRX1200GGPRO	C1/P2	OK
JOZ2	12204M002	2.489	0.024	C1/P2	LEICA GRX1200GGPRO	C1/P2	OK
LAMA	12209M001	2.546	0.020	C1/P2	LEICA GRX1200GGPRO	C1/P2	OK
MATE	12734M008	2.454	0.025	C1/P2	LEICA GRX1200GGPRO	C1/P2	OK
ONSA	10402M004	0.317	0.023	P1/P2	JPS E_GGD	P1/P2	OK
PTBB	14234M001	-0.096	0.027	P1/P2	ASHTECH Z-XII3T	P1/P2	OK
TLSE	10003M009	2.851	0.023	C1/P2	TRIMBLE NETR5	C1/P2	OK
WSRT	13506M005	-0.091	0.022	P1/P2	AOA SNR-12 ACT	P1/P2	OK
WTZR	14201M010	2.503	0.030	C1/P2	LEICA GRX1200GGPRO	C1/P2	OK
WTZZ	14201M014	0.335	0.023	?1/?2	TPS E_GGD	P1/P2	
ZIM2	14001M008	2.891	0.025	C1/P2	TRIMBLE NETR5	C1/P2	OK
ZIMM	14001M004	2.608	0.021	C1/P2	TRIMBLE NETRS	C1/P2	OK

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With the same technology the signal reported in the RINEX3 files for the MGEX stations can be verified and potentially the reference for the “X-signal” for each receiver type (and firmware) determined.

GNSS Phase Biases

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$
$$L_i^k = |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_i + \Delta\vec{\chi}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) \\ + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

GNSS Phase Biases

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On the first view, the phase bias parameters (α_i, α^k) seems to be easily manageable in the GNSS processing because the ambiguity term (N_i^k) is fully correlated and can absorb all effects.

GNSS Phase Biases

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On the first view, the phase bias parameters (α_i, α^k) seems to be easily manageable in the GNSS processing because the **ambiguity term** (N_i^k) is **fully correlated** and can absorb all effects.

This is only true as long as the **ambiguities are not resolved** to their integer values.

Forming Differences

$$L_i^k = |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_i + \Delta\vec{\chi}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) \\ + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

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Forming Differences

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Forming single differences between two stations we obtain:

$$\Delta L_{ij}^k = L_i^k - L_j^k \\ = |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_i + \Delta\vec{\chi}_i)| - |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_j + \Delta\vec{\chi}_j)| \\ + T_i^k - T_j^k - (I_i^k - I_j^k) - c \cdot (\delta_i - \delta_j - \alpha_i + \alpha_j) \\ + \lambda^k \cdot (N_i^k - N_j^k) - \lambda^k \cdot (\varphi_i(t_0) - \varphi_j(t_0))$$

Forming Differences

$$\begin{aligned}\Delta L_{ij}^k &= |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_i + \Delta\vec{\chi}_i)| - |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_j + \Delta\vec{\chi}_j)| \\ &\quad + T_i^k - T_j^k - (I_i^k - I_j^k) - c \cdot (\delta_i - \delta_j - \alpha_i + \alpha_j) \\ &\quad + \lambda^k \cdot (N_i^k - N_j^k) - \lambda^k \cdot (\varphi_i(t_0) - \varphi_j(t_0))\end{aligned}$$

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Double differences between two satellites and receivers result in:

$$\begin{aligned}\nabla \Delta L_{ij}^{kl} &= L_{ij}^k - L_{ij}^l \\ &= |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_i + \Delta\vec{\chi}_i)| - |(\vec{x}^k + \Delta\vec{\chi}^k) - (\vec{x}_j + \Delta\vec{\chi}_j)| \\ &\quad - |(\vec{x}^l + \Delta\vec{\chi}^l) - (\vec{x}_i + \Delta\vec{\chi}_i)| + |(\vec{x}^l + \Delta\vec{\chi}^l) - (\vec{x}_j + \Delta\vec{\chi}_j)| \\ &\quad + T_i^k - T_j^k - T_i^l + T_j^l - (I_i^k - I_j^k - I_i^l + I_j^l) \\ &\quad + \lambda^k \cdot (N_i^k - N_j^k) - \lambda^l \cdot (N_i^l - N_j^l) - (\lambda^k - \lambda^l) \cdot (\varphi_i(t_0) - \varphi_j(t_0))\end{aligned}$$

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GNSS Phase Biases

- The ambiguity resolution in the zero difference processing does also only use double differences to get access to the integer ambiguities.

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Doubts in the consistency are recommended if

- the **two satellites belong to different GNSS** (even if they are using the same frequency: L1 and L5 for GPS and Galileo) because of a potential **Inter-system bias (ISB)**

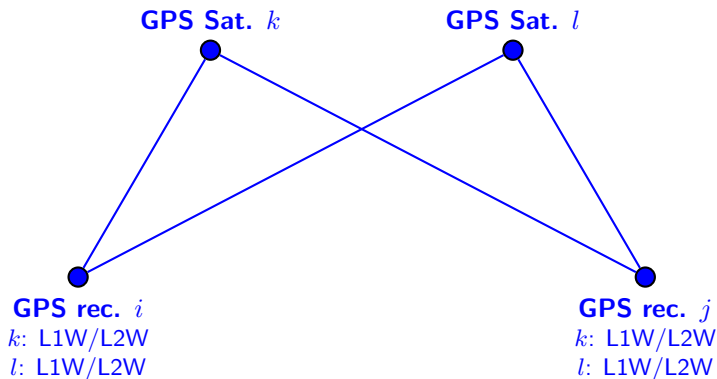
GNSS Phase Biases

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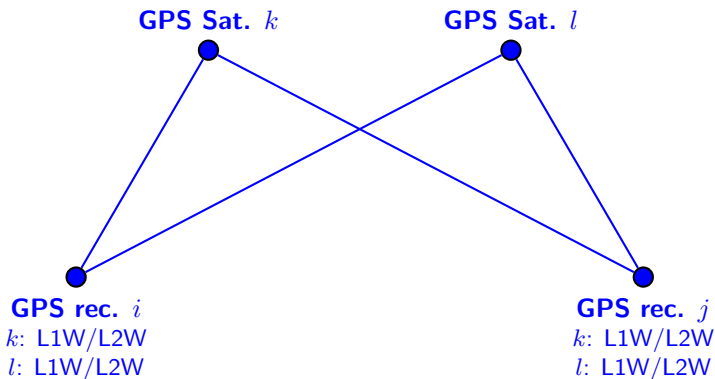
Doubts in the consistency are recommended if

- the **two satellites belong to different GNSS** (even if they are using the same frequency: L1 and L5 for GPS and Galileo) because of a potential **Inter-system bias (ISB)**
- the signals are received on **different frequencies** because different hardware delays are expected (**Inter-frequency bias, IFB**) (alternatively, the IFB may be calibrated and corrected, e.g., for GLONASS ambiguity resolution).

Compatibility of Phase-Related Hardware Delay



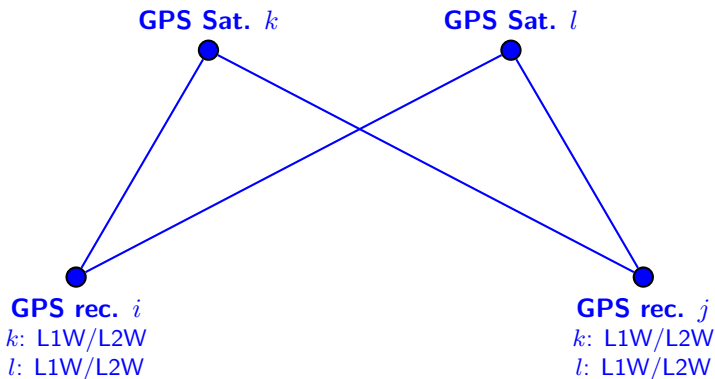
Compatibility of Phase-Related Hardware Delay



k : $\alpha_i(L1W)$ $\alpha_i(L2W)$
 l : $\alpha_i(L1W)$ $\alpha_i(L2W)$

k : $\alpha_j(L1W)$ $\alpha_j(L2W)$
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Compatibility of Phase-Related Hardware Delay

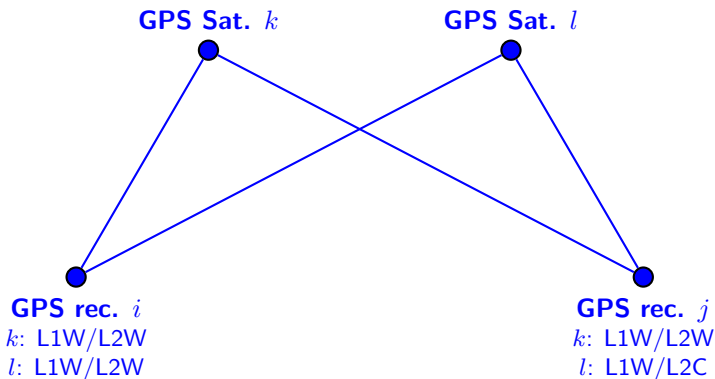


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ambiguity resolution possible

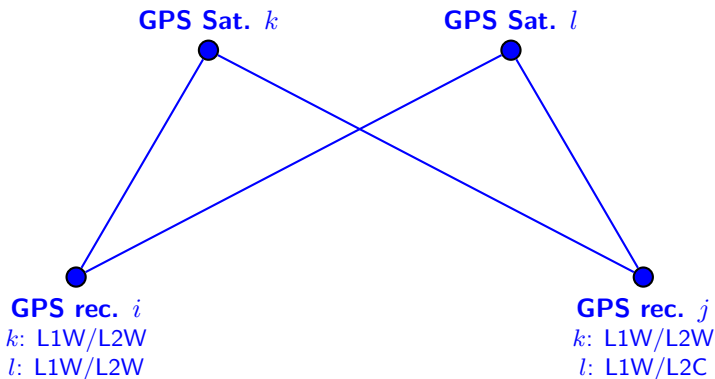
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Compatibility of Phase-Related Hardware Delay

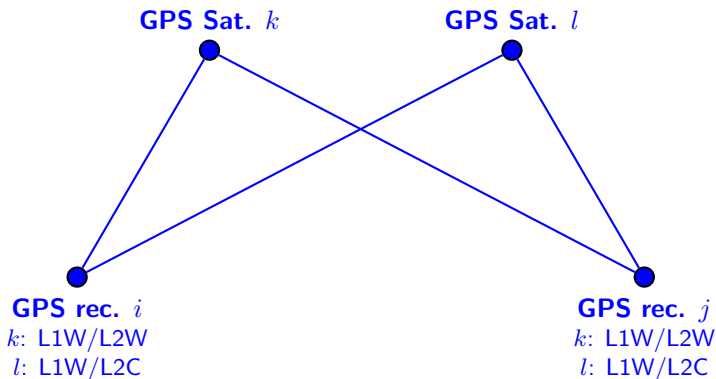


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 l : $\alpha_j(L1W)$ $\alpha_j(L2C)$

"quarter cycle problem" – no resolution

Compatibility of Phase-Related Hardware Delay

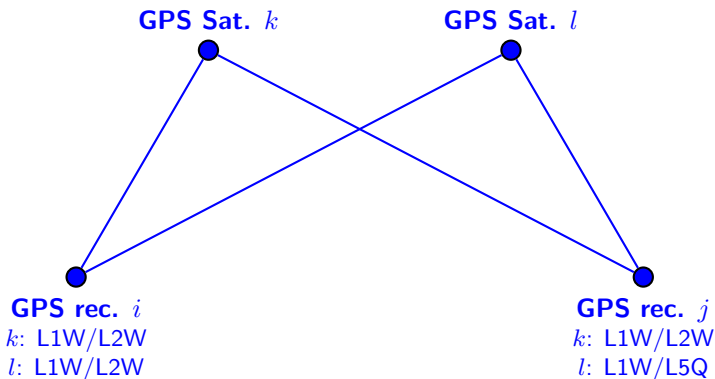


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 l : $\alpha_i(L1W)$ $\alpha_i(L2C)$

k : $\alpha_j(L1W)$ $\alpha_j(L2W)$
 l : $\alpha_j(L1W)$ $\alpha_j(L2C)$

ambiguity resolution possible

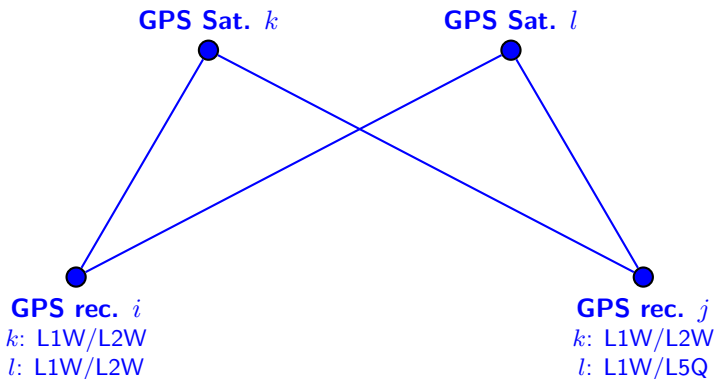
Compatibility of Phase-Related Hardware Delay



k : $\alpha_i(L1W)$ $\alpha_i(L2W)$
 l : $\alpha_i(L1W)$ $\alpha_i(L2W)$

k : $\alpha_j(L1W)$ $\alpha_j(L2W)$
 l : $\alpha_j(L1W)$ $\alpha_j(L5Q)$

Compatibility of Phase-Related Hardware Delay

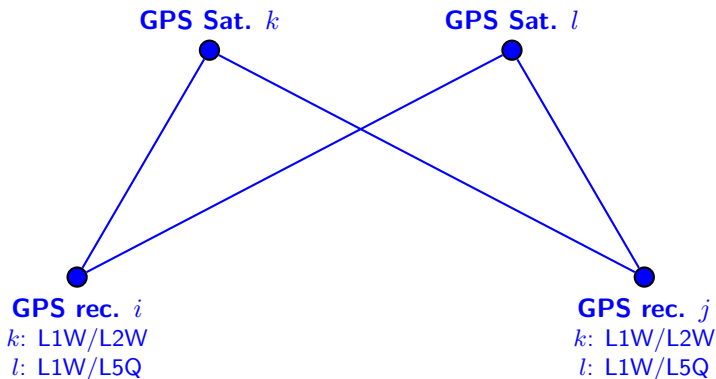


k : $\alpha_i(L1W)$ $\alpha_i(L2W)$
 l : $\alpha_i(L1W)$ $\alpha_i(L2W)$

k : $\alpha_j(L1W)$ $\alpha_j(L2W)$
 l : $\alpha_j(L1W)$ $\alpha_j(L5Q)$

Incompatible – no resolution

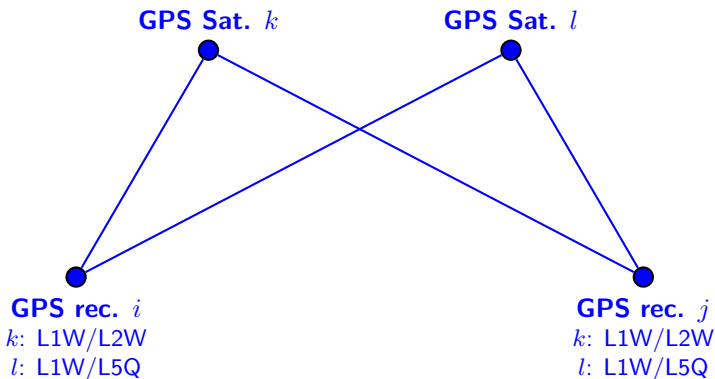
Compatibility of Phase-Related Hardware Delay



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k : $\alpha_j(L1W)$ $\alpha_j(L2W)$
 l : $\alpha_j(L1W)$ $\alpha_j(L5Q)$

Compatibility of Phase-Related Hardware Delay

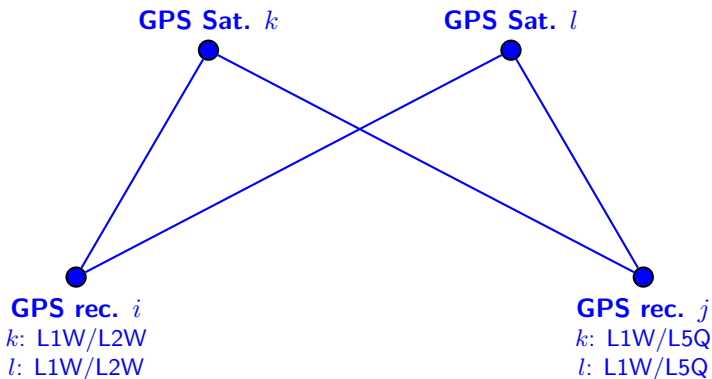


k : $\alpha_i(L1W)$ $\alpha_i(L2W)$
 l : $\alpha_i(L1W)$ $\alpha_i(L5Q)$

k : $\alpha_j(L1W)$ $\alpha_j(L2W)$
 l : $\alpha_j(L1W)$ $\alpha_j(L5Q)$

Be careful: $\alpha_i(L5Q) - \alpha_i(L2W) \stackrel{?}{=} \alpha_j(L5Q) - \alpha_j(L2W)$

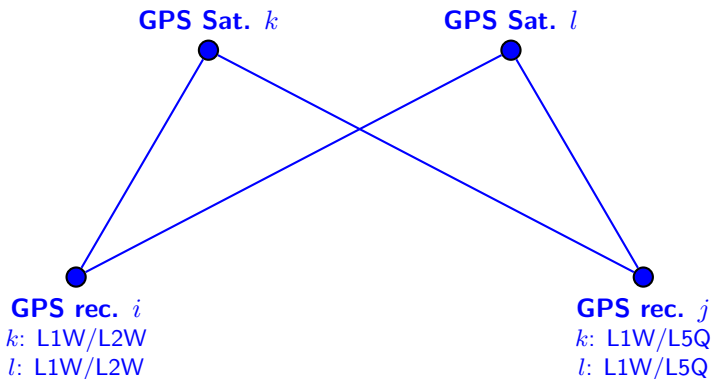
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Compatibility of Phase-Related Hardware Delay

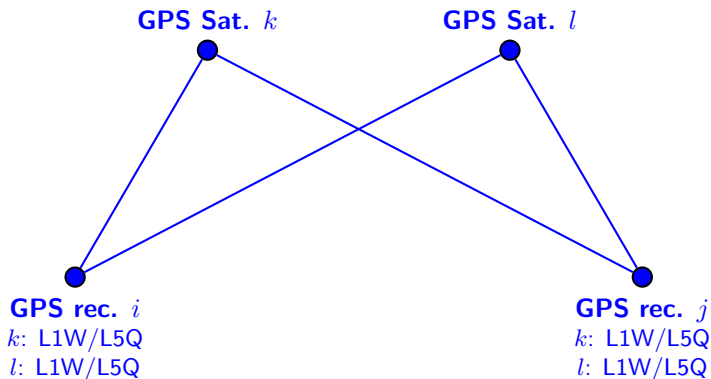


k : $\alpha_i(L1W)$ $\alpha_i(L2W)$
 l : $\alpha_i(L1W)$ $\alpha_i(L2W)$

k : $\alpha_j(L1W)$ $\alpha_j(L5Q)$
 l : $\alpha_j(L1W)$ $\alpha_j(L5Q)$

Be careful: $\alpha^k(L5Q) - \alpha^k(L2W) \stackrel{?}{=} \alpha^l(L5Q) - \alpha^l(L2W)$

Compatibility of Phase-Related Hardware Delay

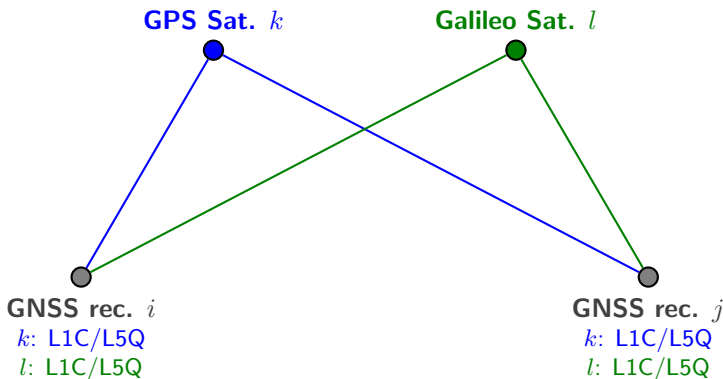


k : $\alpha_i(L1W)$ $\alpha_i(L5Q)$
 l : $\alpha_i(L1W)$ $\alpha_i(L5Q)$

k : $\alpha_j(L1W)$ $\alpha_j(L5Q)$
 l : $\alpha_j(L1W)$ $\alpha_j(L5Q)$

ambiguity resolution possible

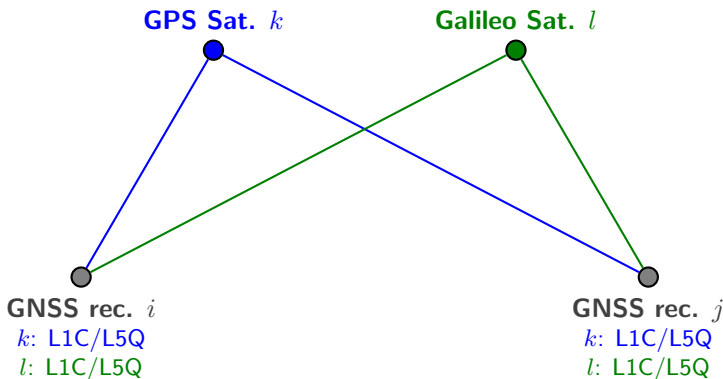
Compatibility of Phase-Related Hardware Delay



$$\begin{array}{ll} \alpha_i(L1C)^{GPS} & \alpha_i(L5Q)^{GPS} \\ \alpha_i(L1C)^{GAL} & \alpha_i(L5Q)^{GAL} \end{array}$$

$$\begin{array}{ll} \alpha_j(L1C)^{GPS} & \alpha_j(L5Q)^{GPS} \\ \alpha_j(L1C)^{GAL} & \alpha_j(L5Q)^{GAL} \end{array}$$

Compatibility of Phase-Related Hardware Delay



$$\alpha_i(L1C)^{GPS}$$

$$\alpha_i(L1C)^{GAL}$$

$$\alpha_i(L5Q)^{GPS}$$

$$\alpha_i(L5Q)^{GAL}$$

$$\alpha_j(L1C)^{GPS}$$

$$\alpha_j(L1C)^{GAL}$$

$$\alpha_j(L5Q)^{GPS}$$

$$\alpha_j(L5Q)^{GAL}$$

Be careful: $ISB_i(L1C, L5Q) \stackrel{?}{=} ISB_j(L1C, L5Q)$

Dependency of the Terms

$$P_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k + I_i^k + c \cdot (\delta_i - a_i) - c \cdot (\delta^k - a^k)$$

$$L_i^k = |(\vec{x}^k + \Delta\vec{x}^k) - (\vec{x}_i + \Delta\vec{x}_i)| + T_i^k - I_i^k + c \cdot (\delta_i - \alpha_i) - c \cdot (\delta^k - \alpha^k) + \lambda^k \cdot N_i^k + \lambda^k \cdot \Delta\varphi_i^k$$

GNSS:

Code
Phase

$\Delta\vec{x}_i$
 $\Delta\vec{x}_i$

a_i
 α_i

δ^k
 δ^k

ISB: Inter-System Bias

Frequency:

Code
Phase

$\Delta\vec{x}^k$ $\Delta\vec{x}_i$
 $\Delta\vec{x}^k$ $\Delta\vec{x}_i$

a_i a^k
 α_i α^k

IFB: Inter-Frequency Bias

Signal type:

Code

a_i a^k

DCB: Differential Code Bias

GPS–GLONASS Antenna Bias: Coordinates

- A GNSS antenna should be individually calibrated for each GNSS to consider the system-dependency of the $\Delta\vec{\chi}_i$ term.

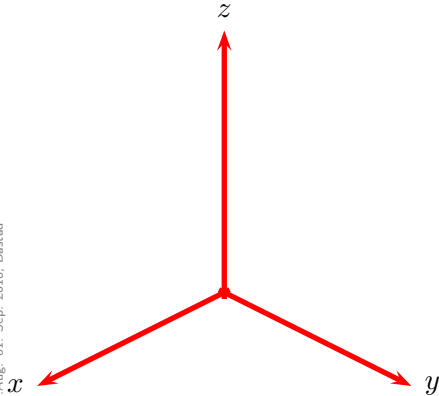
GPS–GLONASS Antenna Bias: Coordinates

- A GNSS antenna should be individually calibrated for each GNSS to consider the system-dependency of the $\Delta\vec{\chi}_i$ term.
- The coordinate **GLONASS-GPS translation bias** shall compensate for a potential deficiency in the GNSS-specific calibration of the antenna phase center offset.

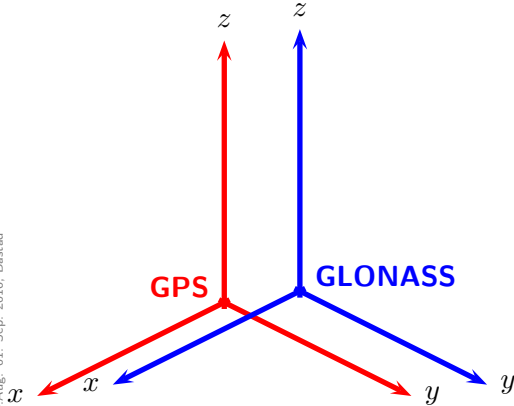
GPS–GLONASS Antenna Bias: Coordinates

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- The coordinate **GLONASS-GPS translation bias** shall compensate for a potential deficiency in the GNSS-specific calibration of the antenna phase center offset.
- A related bias parameter was implemented for a background test solution at the CODE analysis center in early 2011.

GPS–GLONASS Antenna Bias: Coordinates

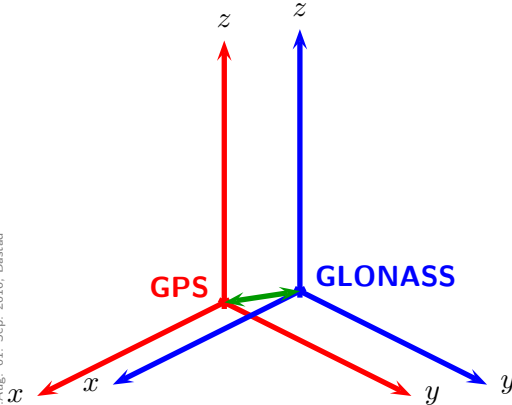


GPS–GLONASS Antenna Bias: Coordinates



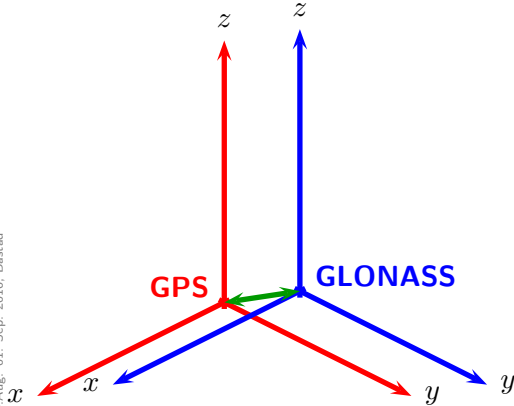
- Station coordinate from GPS-only
- Station coordinate from GLONASS-only

GPS–GLONASS Antenna Bias: Coordinates



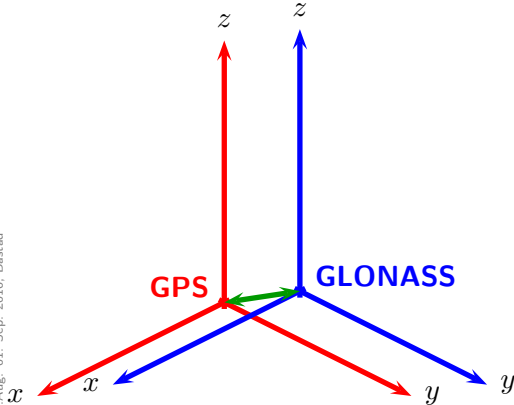
- Station coordinate from GPS-only
- Station coordinate from GLONASS-only
- Vector between GPS– and GLONASS–coordinates

GPS–GLONASS Antenna Bias: Coordinates



- Station coordinate from GPS-only
- Station coordinate from GLONASS-only
- Vector between GPS– and GLONASS–coordinates
- two independent networks with independent datum definition

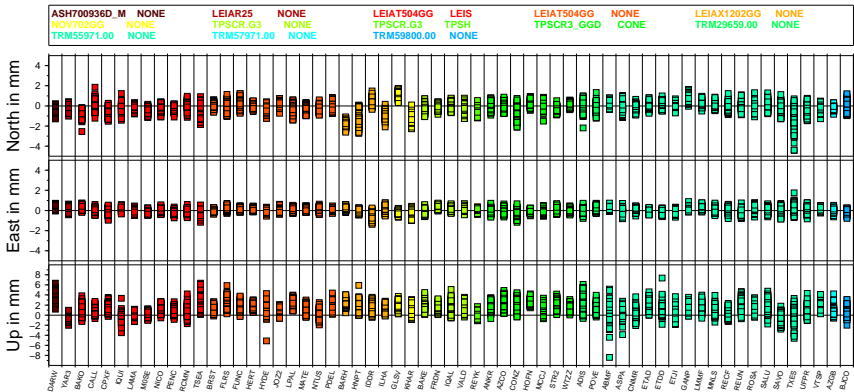
GPS–GLONASS Antenna Bias: Coordinates



- Station coordinate from GPS-only
- Station coordinate from GLONASS-only
- Vector between GPS– and GLONASS–coordinates
- two independent networks with independent datum definition
- zero–mean condition over all GPS–GLONASS–bias in xyz

GPS–GLONASS Antenna Bias: Coordinates

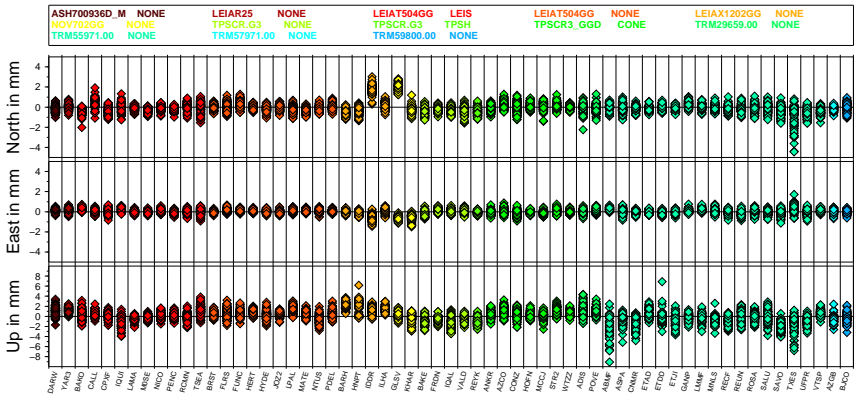
Differences between weekly coordinate solutions for GPS/GLONASS stations with and without estimating GLONASS-GPS translation biases:



GPS–GLONASS–Bias for the coordinates using IGS05.atx–antenna phase center corrections from weekly solutions of the years 2009 and 2010.

GPS–GLONASS Antenna Bias: Coordinates

Differences between weekly coordinate solutions for GPS/GLONASS stations with and without estimating GLONASS-GPS translation biases:



GPS–GLONASS–Bias for the coordinates using IGS08.atx–antenna phase center corrections from weekly solutions of the years 2009 and 2010.

GPS–GLONASS Antenna Bias: Troposphere

The **troposphere GLONASS-GPS translation bias** shall compensate for a potential deficiency in the GNSS-specific calibration of the antenna phase center variation.

GPS–GLONASS Antenna Bias: Troposphere

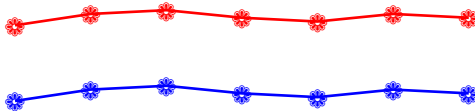
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GPS–GLONASS Antenna Bias: Troposphere

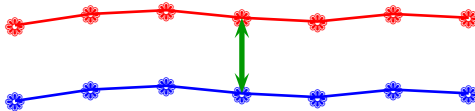
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- Troposphere estimates from GPS-only
- Troposphere estimates from GLONASS-only



GPS–GLONASS Antenna Bias: Troposphere

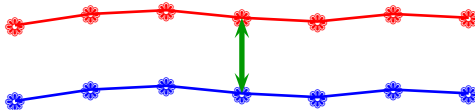
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- Difference between GPS– and GLONASS–troposphere series

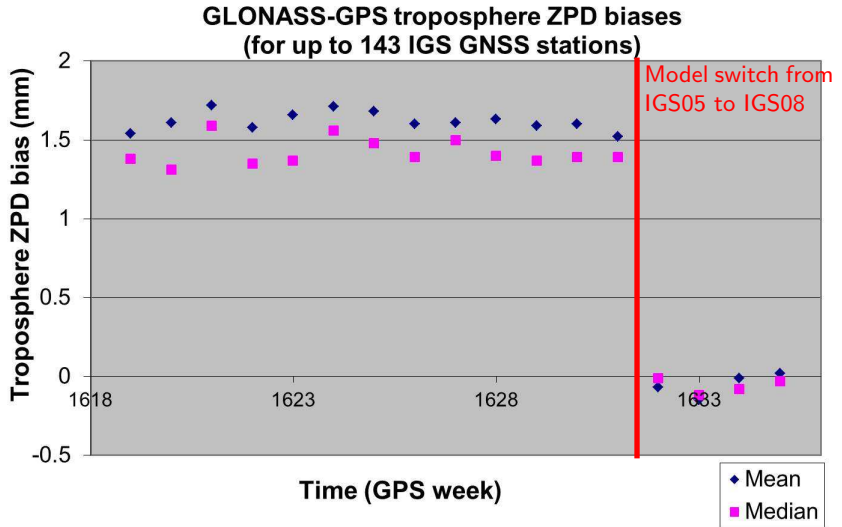
GPS–GLONASS Antenna Bias: Troposphere

The **troposphere GLONASS-GPS translation bias** shall compensate for a potential deficiency in the GNSS-specific calibration of the antenna phase center variation.



- Troposphere estimates from GPS-only
- Troposphere estimates from GLONASS-only
- Difference between GPS– and GLONASS–troposphere series
- No constraints on the GPS–GLONASS–bias are needed

GPS–GLONASS Antenna Bias: Troposphere



Inter-System Antenna Bias

- The demonstrated way is one option to compensate for deficiencies in the (receiver) antenna calibration.

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Inter-System Antenna Bias

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- The currently used IGS08.atx and IGS14.atx sets of corrections provide sufficient calibration for legacy GPS and GLONASS measurements.
- **The missing receiver antenna calibration values are a significant problem in the current status of multi-GNSS processing.**
- With the proposed method the influence of the deficiency on the results may be limited given that a sufficient amount of data are available.

THANK YOU

for your attention



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